

Phonetic and Phonological Posterior Search Space Hashing Exploiting Class-Specific Sparsity Structures

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Abstract

This paper shows that exemplar-based speech processing using class-conditional posterior probabilities admits a highly effective search strategy relying on posteriors' intrinsic sparsity structures. The posterior probabilities are estimated for phonetic and phonological classes using deep neural network (DNN) computational framework. Exploiting the class-specific sparsity leads to a simple quantized posterior hashing procedure to reduce the search space of posterior exemplars. To that end, small number of quantized posteriors are regarded as representatives of the posterior space and used as hash keys to index subsets of neighboring exemplars. The k nearest neighbor (kNN) method is applied for posterior based classification problems. The phonetic posterior probabilities are used as exemplars for phonetic classification whereas the phonological posteriors are used as exemplars for automatic prosodic event detection. Experimental results demonstrate that posterior hashing improves the efficiency of kNN classification drastically. This work encourages the use of posteriors as discriminative exemplars appropriate for large scale speech classification tasks.

Index Terms: Fast *k*NN, Structured sparsity, Quantized posterior hashing, Posterior representatives, Phonetic classification, Automatic prosodic event detection.

1. Introduction

Exemplar-based speech processing provides a powerful big data solution for potentially a wide range of speech applications. In particular, speech classification relying on exemplar matching possesses higher flexibility than the statistical methods due to lack of prejudices on data and expected answers. The fundamental question that yet remains is the application-specific appropriate choice of exemplars. The present manuscript reinforces the position of deep neural network (DNN) based class-conditional posterior probabilities (hereafter referred to as *posteriors*) as a great choice of exemplars for speech classification tasks.

In theory, if infinite number of exemplars of continuous probability density functions are provided, a simple nearestneighbor rule leads to optimal classification [1]. In the context of speech recognition, the nearest-neighbor based techniques have been used as non-parametric methods to perform classconditional posterior probability estimation for acoustic modeling [2, 3]. Typical choice of exemplars are variants of spectral features [4, 5], and approximate neighborhood search strategies are tailored to provide tractable frameworks [2].

Application of hashing in nearest neighbor search enables splitting the search space into buckets each identified with a unique hash key. The exhaustive search space is thus downsized to the corresponding bucket sizes [6]. In this context, the hash function ensures locality preserving of similar/neighboring data while the whole space is spanned in disjoint splits [7]. In posterior space, as we will see further in this paper, all above essential features are obtained through a simple *linear posterior quantization* to generate the hash keys as posterior representatives, and populate the corresponding buckets of neighboring posterior vectors.

DNN posteriors live in union of low-dimensional/structured sparse subspaces [8, 9]. Exploiting this property enables hierarchical speech recognition and classification frameworks based on sparse modeling of phonetic posterior exemplars [10, 11]. Furthermore, the low-dimensional subspaces can be modeled through dictionary learning for sparse representation, and projection of the posteriors into the space characterized over the training data reduces the mismatch of the testing posteriors, and leads to enhanced acoustic modeling for speech recognition [8, 9]. In addition to the phonetic posteriors, our previous studies on phonological posteriors show that they conform to a small number of unique binary structures which are a tiny fraction of the number of permissible codes [12]. Exploiting this property enables construction of a small-size codebook for very low-bit rate speech coding [12, 13]. More recently, we also found structured sparsity of phonological posteriors highly effective for classification of supra-segmental linguistic events [14].

In this paper, we propose a novel application of structured sparsity of posterior probabilities in devising an effective hashing technique to reduce the search space of posterior exemplars. Motivated by the idea of locality sensitive hashing for fast neighborhood search [7], the geometric locality in the space of posteriors can be defined by thresholding the high probability components at multiple quantized levels. As the variability in the space of posteriors is largely confined to the underlying class probabilities, grouping the posteriors according to their quantized codes ensures the actual neighbors in disjoint buckets. The posteriors are investigated at two levels corresponding to phonetic and phonological classes. In the former case phonetic classification is evaluated, whereas in the latter case automatic prosodic event detection is performed, both based on k nearest neighbor (kNN) search using the quantized posterior hashing technique.

In the rest of the paper, the posterior hashing theory is described in Section 2. Experimental studies are carried out in Section 3, and the conclusions are drawn in Section 4 with an outlook to development of large scale, fast and flexible speech applications relying on DNN posterior exemplars.

2. Quantized Posterior Hashing

Inspired from the idea of locality sensitive hashing [7], a deterministic procedure for posterior space hashing is proposed. This procedure relies on structured sparsity of posterior subspaces to characterize the geometric localities, and enables search space reduction for neighborhood analysis of posterior exemplars.

2.1. Structured Sparsity

Phonetic and phonological posterior estimation requires speech analysis that turns a sequence of N acoustic feature observations $X = \{x_1, \dots, x_n, \dots, x_N\}$ into a sequence of N posterior probability vectors $Z = \{z_1, \dots, z_n, \dots, z_N\}$ where

$$\boldsymbol{z}_n = [p(C_1|\boldsymbol{x}_n), \dots, p(C_q|\boldsymbol{x}_n), \dots, p(C_Q|\boldsymbol{x}_n)]^\top$$

consists of Q class-conditional posterior probabilities, and .^{\top} denotes the transpose operator. DNN is the state-of-the-art computational method to estimate the posterior probabilities. A single DNN is employed to estimate the phonetic posteriors. As for the phonological posteriors, a binary classifier DNN is used for estimation of any individual class probability; thus the output of multiple parallel DNNs are concatenated to form the phonological posterior (details in 3.1–3.2).

Figure 1 depicts a sample of phonological and phonetic posteriors estimated for an utterance of speech signal. The left plots illustrate the binary quantized posteriors of the continuous probabilities depicted in the right plots. An exclusive class-specific sparsity structure is evident for phonetic posteriors which is pertained to the DNN exclusive mapping to the hard output phonetic labels. As a result, the class-specific subspaces are highly structured, and the matrices of class-specific phonetic posteriors have a very low-rank [8, 9]; the phonetic posteriors live in union of these low-dimensional subspaces.

On the other hand, the restricted multi-class probabilities are visible at phonological posteriors. As the phonological classes correspond to sub-phonetic attributes, multiple classes are activated for generation of a sub-word unit, however, their combination is confined to a small permissible activation of articulatory mechanisms as determined in a phonological system (for example the well-known Sound Pattern of English [15]). These permissible combinations define the sparsity structures underlying phonological posteriors [12]. In both phonetic and phonological illustrations, the sparse vectors exhibit a sequencing structure inherited from the input acoustic feature observations. More details about the DNN setup for estimation of posteriors, their dimension and databases will be described in Sections 3.1–3.2.

2.2. Quantized Posterior Representatives are Hash Keys

Relying on the structured sparsity of posteriors, we devise a hashing technique to divide the space into smaller size buckets of neighboring posteriors.

As already discussed in Section 2.1, posterior exemplars are sparse vectors living in union of low-dimensional subspaces. Hence, for any posterior vector, the probabilities are confined to a very small number of components where the indices of high probabilities identify the unique structure of the underlying subspace. Accordingly, the number of unique quantized posteriors is relatively small with respect to the sample size, and the quantized posteriors can be regarded as representatives of the posterior space. The quantized posterior representatives are used as hash keys for splitting the space into geometric neighbors. The following hashing formula expresses this method through



Figure 1: Posteriograms of phonological and phonetic posteriors. Quantized posteriors are representatives of the posterior space that can be used as the hash keys for effective nearest neighbor search.

different levels of quantization.

$$H(\boldsymbol{z}) = \frac{\left\lfloor 2^{b} \boldsymbol{z} \right\rfloor}{2^{b}} \tag{1}$$

where z is a posterior probability vector, and b is the number of bits for quantization.

The quantized posterior hashing divides the search space into disjoint buckets where the number of buckets is proportional to the number of classes. In theory, the number of classes is equal to the dimension of DNN outputs for phonetic posteriors, or equal to the number of permissible combinations of the phonological classes as defined in the phonological system. Our experimental studies conducted in Section 3.3 demonstrate this proportionality. As the number of permissible combinations is relatively large in a phonological system, we will see in Section 3.4 that even the binary posterior hashing leads to effectively small-size buckets encapsulating similar posterior exemplars.

As the number of quantization bits b is increased, the buckets will define finer localities. By fixing a minimum bucket size, a hierarchical hashing can be devised for search space indexing, and the neighborhood search is accomplished for the finest matched quantization key (details in 3.3).

This hashing technique can be combined with kNN to enable efficient posterior classification. In this approach, the quantized posteriors are used to identify the neighboring exemplars (the relevant bucket) while kNN is performed on continuous representations. We will see in Sections 3.3–3.4 that this simple hashing idea can reduce the search space of posteriors drastically.

2.3. Analysis and Cost

In theory, quantization of every component of posteriors in b bits leads to splitting the space in maximum $K = 2^b Q$ disjoint regions. Accordingly, the size of training data in each bucket can be reduced to an average $N/2^K$. The minimum similarity occurs for the vectors at the boundaries; therefore, the maximum distance of the two vectors z_1 and z_2 with equal hash keys is approximately

$$d(H(\boldsymbol{z_1}), H(\boldsymbol{z_1}) + \frac{1}{2^b} \boldsymbol{1}_K)$$

where $\mathbf{1}_K$ is an all-ones vector of dimension K. Hence, the probability of negative examples in a bucket is equal to the probability of having two values closer than $\frac{1}{2^b}$ in every dimension. Since the posteriors are between 0 and 1, this probability is $p = \frac{1}{2^b}$. The negative examples occur when the K-dimensional keys of the two posteriors of different classes are equivalent, therefore, negative examples have the probability of $1 - p^K$. Since the typical number of Q is often more than 10, this hashing function leads to a very small probability of encapsulating negative examples or similarly wrong positive examples in the same bucket.

In practice, the number of non-empty buckets is very small, and by considering a large minimum number of exemplars per bucket, the number of effective hash keys for each class is proportional to $\|\lfloor 2^b E(\boldsymbol{z}|C_q) \rfloor\|_0$, where $E(\boldsymbol{z}|C_q)$ denotes the ensemble average of the posterior vectors belonging to class C_q , and $\|.\|_0$ is the number of non-zero components. The total number of hash keys is thus related to $\sum_{q=1}^Q \|\lfloor 2^b E(\boldsymbol{z}|C_q) \rfloor\|_0$.

3. Experimental Results

In this section, we evaluate the effectiveness of hashing for neighborhood search of posterior exemplars. Two kNN tasks are investigated, namely, phonetic classification using phone posteriors, and automatic prosodic event detection using phonological posteriors.

3.1. DNN Setup for Phonetic Posteriors

The phonetic classification is conducted on AMI corpus [16]. A DNN is used to estimate the phonetic posterior probabilities, and implemented using Kaldi toolkit [17]. Its architecture consists of three hidden layers with 1024 nodes. The input features of the DNN are Mel-frequency cepstral coefficients (MFCC) concatenated with the first and second order dynamic features using a context of 9 frames, and estimated for every 10ms of speech. The DNN outputs are hard labels corresponding to 43 dimensional English phonetic classes. The training labels are obtained from hidden Markov model (HMM) force alignment using speech transcription. We use the standard splitting of training, development and test data as performed in [18].

3.2. DNN Setup for Phonological Posteriors

The Wall Street Journal WSJ0 and WSJ1 continuous speech recognition corpora [19] are used for training the phonological class detectors. Phonological detectors are trained on the training set *si_tr_s_284* including 37,514 utterances using the Government Phonology (GP) phonological features [20, 21]. For each phonological class, a 3x1024 DNN is initialized by deep belief network pre-training of [22], and trained using Kaldi toolkit. The DNN output is trained as either 1 or 0 if the phonological class is present or not. Hence, each DNN estimates the probability of occurrence of one phonological class. The outputs of all DNNs are concatenated to form a phonological posterior vector.

To perform prosodic event detection experiments, the GP posteriors are estimated on a labeled subset taken from the SI-WIS database [23]. The dimension of phonological posteriors is 12 according to the GP phonological system that consists of the three basic resonance phonological primes commonly labeled as A, U, I, denoting the peripheral vowel qualities [a], [u] and [i] respectively. Other vowels are defined by a composition of the basic ones, such as [e] results in fusing the I and A primes. In addition to these 'vocalic' primes, GP proposes also the 'con-

sonantal' primes. The evaluation data consists of recordings of 10 training and 3 testing English speakers. Each speaker reads about 25 sentences, among which 5 questions, with focus (emphasis) on one predefined word. The corresponding transcription for each sentence was given, with a tag on the words that the speakers were asked to emphasize. Hence, the goal of prosodic event detection is basically detection of emphasized segments in an utterance where the boundary of the segments are known beforehand, i.e. a top-down detection scenario.

3.3. Fast kNN for Phonetic Classification

The cosine similarity is used in kNN search for phonetic classification [24]. The value of k for exhaustive search kNN is chosen as 150; for hashing-based kNN at binary level, it is chosen as 20, and for higher levels, it is 11 using the 10-fold cross validation. We perform classification of a random selection of 50k test posteriors using the labeled development posteriors.

The hash keys are obtained at different quantization levels. The minimum bucket size is fixed to 500, so if a hash key results in less than 500 neighborhood posteriors, it is discarded. For any test posterior, hashing can be implemented in a hierarchical procedure. The test hash keys at multiple quantization levels are obtained and compared with the available hash keys of labeled data using Jaccard similarity [25], then the finest matched key with Jaccard similarity = 1 is used to determine the bucket of neighboring posteriors. This procedure leads to multi-level hashing (mul-h). Alternatively, the single level quantization codes are used to obtain the hash keys where the bucket with the closest key (even if the Jaccard similarity is smaller than 1) is used for neighborhood search. This procedure leads to single level hashing (sin-h). Once the bucket of neighboring posteriors is identified, kNN is performed on continuous representations. The results of kNN phonetic classification performance are listed in Table 1.

Table 1: *kNN Phonetic classification accuracy using single level (sin-h) and multi-level (mul-h) quantized posterior hashing on AMI database.*

b	#Buc.	Search size	Ac. (sin-h)	Ac. (mul-h)
64	1	3'174'011	70.3%	70.3%
1	42	60'447	69.9%	69.9%
2	319	9'371	69.6%	69.9%

We observe that when the number of buckets is very small, and the search space can be reduced drastically (by a factor of \sim 319 using 2 bits quantization) with small degradation in *k*NN classification accuracy. At 2 bits quantization level, the ratio of posteriors with a similar hash key is 94.2%. The hash keys can be stored as binary vectors to enable fast binary matching to find the appropriate bucket, and parallel matching of the hash keys at multiple levels minimizes the computational overhead. In addition, the testing posteriors with different hash keys can be processed independently in parallel streams that can lead to higher speed up in exemplar based frameworks.

3.4. Fast kNN for Automatic Prosodic Event Detection

The information of linguistic and prosodic events at suprasegmental level is encoded in phonological attributes, thus classification of higher-level events (such as lexical stress or prosodic accent) is feasible exploiting the structure of high probability phonological posteriors [14]. In this section, we study emphasis detection based on nearest neighbor search using phonological posteriors; Jaccard similarity [25] is used to



Figure 2: Distinct structured sparsity of phonological posteriors depicted for two pronunciation of the phoneme "I" in unemphasized and emphasized words.

find the nearest neighbor.

This method relies on the hypothesis that phonological posteriors encode information about the emphasized or unemphasized speech utterances in the support of their high probability components. The support can be identified using quantization at different levels. Figure 2 illustrates an example of binary structures underlying un-emphasized and emphasized realizations of phoneme "I". The difference in the binary patterns is evident. To visualize this property in a larger scale, we plot the t-distributed stochastic neighbor embedding (tSNE) [26] of arbitrary selection of 1000 frames of phonological posteriors with and without emphasis in Figure 3.

This empirical observation suggests that the binary structures of phonological posteriors are indicative of their emphasized nature, thus they can be regarded as representatives of emphasis and un-emphasis variability of phonological posteriors. Accordingly, the binary structures are used as the hash keys to split the space into buckets of neighboring exemplars. The nearest neighbor rule is then used for emphasis detection on a frame basis; the frame-level decisions are pulled within the known boundaries to make a supra-segmental decision based on majority counting. The results are listed in Table 2.

Table 2: *Emphasis detection using phonological posterior hashing on SIWIS database.*

b	#Buckets	Avg bucket-size	Accuracy
64	1	100'284	87.1%
1	405	222	93.5%

We can see that the search space of posterior exemplars is reduced by extracting the binary codes, however, the number of buckets (unique hash keys) is more than the binary codes of phonetic posteriors. This can be explained due to the definition and training of phonological posteriors which results in high probability components corresponding to multiple phonological classes (as opposed to phonetic posteriors which often have a single high probability component).

Furthermore, unlike phonetic posterior hashing, we do not enforce any constraint on the bucket size since the best value of k is found to be 1 for this task. During the nearest neighbor search, if a binary code does not perfectly match the training hash keys, the most similar code quantified in terms of Jaccard similarity is used. We can see that *binary* hashing of phonological posteriors enables restriction of the search space to the more "correct" exemplars as the classification improves through this confined search.



Figure 3: tSNE visualization of binary phonological posteriors with and without emphasis.

4. Conclusions and Future Directions

Posterior exemplars are sparse and live in union of lowdimensional subspaces. In this paper, a novel application of this property was proposed by introducing the quantized posterior hashing technique to enable an effective search strategy confined to the local neighborhood of posterior exemplars. The quantized posteriors are regarded as the representatives of the posterior space. It was shown that the number of unique hash keys or equivalently the number of buckets is very small that leads to tremendous reduction of the search space with negligible overhead. This method enables very fast and accurate kNN search for phonetic classification and automatic prosodic event detection.

The number of unique hash keys or different buckets is related to the sparsity level or the number of permissible classes. Since the "optimal" phonetic posteriors indicate a single highly probable class, the number of buckets is proportional to the number of phones. In contrast, the phonological posteriors are indicative of sub-phonetic attributes presented at multiple phonological class probabilities, hence, the number of unique hash keys is proportional to the size of permissible combinations as roughly quantified at binary quantization. In fact, binary level hashing is found very efficient for neighborhood search of phonological posterior exemplars.

Future work will focus on development of fast and flexible large scale ASR in a hierarchical exemplar based framework relying on the generic low-dimensional properties of DNN posterior exemplars. Furthermore, we will investigate other suprasegmental linguistic event detection tasks using structured sparsity of phonological posteriors. Higher semantic information can be integrated with the bottom-up approach towards development of exemplar based ASR framework that can exploit broad contextual information. Moreover, the neural network posterior estimation can be seen as a hash function of any type of speech acoustic features such as spectral features. Hence, exemplarbased speech classification can potentially benefit from the proposed quantized posterior hashing method at any speech representation level. We will study this idea in future developments.

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