

# Optimum Wirelessly Powered Relaying

Caijun Zhong, *Senior Member, IEEE*, Gan Zheng, *Senior Member, IEEE*, Zhaoyang Zhang, *Member, IEEE*, and George K. Karagiannidis, *Fellow, IEEE*

**Abstract**—This letter maximizes the achievable throughput of a relay-assisted wirelessly powered communications system, where an energy constrained source, assisted by an energy constrained relay and both powered by a dedicated power beacon (PB), communicates with a destination. Considering the time splitting approach, the source and relay first harvest energy from the PB, which is equipped with multiple antennas, and then transmits the information to destination. Simple closed-form expressions are derived for the optimal PB energy beamforming vector and time split for energy harvesting and information transmission. Numerical results and simulations demonstrate the superior performance compared with some intuitive benchmark beamforming scheme. Also, it is found that placing the relay at the middle of the source-destination path is no longer optimal.

**Index Terms**— Beamforming, dual-hop relaying, WPC.

## I. INTRODUCTION

GIgabit wireless access will be a reality in fifth generation (5G) wireless systems, with a series of breakthroughs, such as massive multiple-input and multiple-output (MIMO), full-duplex communication and small cell architectures, which in turn, has fueled a number of emerging wireless services, such as mobile gaming, mobile TV and mobile Internet. Furthermore, with the proliferation of smartphones and tablets, one of the most critical issues affecting the user experience is the limited operation lifetime of mobile devices, due to finite battery capacity. Motivated by this, radio-frequency (RF) based energy harvesting technique has received a substantial research interest in recent years [1], [2]. Empowered with the RF energy harvesting capability, it is possible to virtually provide

perpetual energy supply to mobile devices, eliminating the need to plug into the power grid for battery recharging.

RF energy harvesting, combined with information transfer, has resulted in a new emerging topic, namely, simultaneous wireless information and power transfer (SWIPT), which has attracted significant attention from academia and recently from industry. Thus far, various aspects of SWIPT systems have been investigated, including information theoretical limits [3], [4], practical architectures [5]–[7], effect of imperfect channel state information [8], orthogonal frequency division multiplexing (OFDM)-based SWIPT systems [9], [10] and relay-assisted SWIPT systems [11]–[17]. It is worth pointing out here that all these prior works assume that the mobile devices harvest energy from ambient RF signals. However, even if this may be viable for low power devices such as sensors, it is in general infeasible to power larger devices such as smartphones, tablets and laptops [18]. Responding to this key limitation, the authors in [19] proposed a novel network architecture, where cellular base stations are underlaid by dedicated power beacons (PB), which can be used to supply energy to mobile devices through microwave power transfer. Since the PBs do not require any backhaul link, the associated cost of PB deployment is much lower, hence, dense deployment of PBs to ensure network coverage for a wide range of mobile devices is feasible.

In this letter, we consider a dual-hop decode-and-forward (DF) relaying system, where both the source and relay are powered by the dedicated PB. To improve the energy transfer efficiency, the multiple antenna enabled PB performs energy beamforming. It is assumed that wireless power transfer is performed over the same frequency as information transfer, and the time-switching protocol [5] is adopted. As such, the single antenna at the source and relay switches between two hardware chains, one for energy harvesting and one for information transmission/reception. Therefore, the entire communication block consists of two different phases, i.e., energy harvesting phase, where the source and relay harvest the energy from the PB, and information transfer phase, where the relay assists the information transmission between the source and destination.

The main contribution of this letter is the derivation of simple closed-form expressions for the optimal time split between the energy harvesting and information transfer phase, as well as the optimal energy beamforming vectors at the PB, which maximize the system's throughput. Simulation results demonstrate that the optimal solution substantially outperforms the intuitive benchmark beamformer. In addition, it is revealed that placing the relay in the middle of the source and destination path is no longer optimal, instead, the distances to the PB should also be taken into consideration when optimizing the relay position.

**Notations:**  $(\cdot)^*$  denotes the complex conjugate,  $(\cdot)^T$  denotes the matrix transpose, and  $(\cdot)^\dagger$  denotes the Hermitian transpose. **I**

Manuscript received April 06, 2015; accepted April 27, 2015. Date of publication May 01, 2015; date of current version May 08, 2015. This work was supported by the National Key Basic Research Program of China under Grant 2012CB316104, the National Natural Science Foundation of China under Grant 61201229, the Zhejiang Science and Technology Department Public Project under Grant 2014C31051, and by the Zhejiang Provincial Natural Science Foundation of China under Grant LR15F010001. The work of G. K. Karagiannidis was supported by the European Social Fund - ESF and Greek national funds through the Operational Program "Education and Lifelong Learning" of the National Strategic Reference Framework (NSRF) - Research Funding Program: THALES-NTUA MIMOSA. The associate editor coordinating the review of this manuscript and approving it for publication was Prof. Xin Wang.

C. Zhong and Z. Zhang are with the Institute of Information and Communication Engineering, Zhejiang University, Hangzhou, Zhejiang 310027, China (e-mail: caijunzhong@zju.edu.cn).

G. Zheng is with the School of Computer Science & Electronic Engineering, University of Essex, Colchester CO4 3SQ, U.K. (e-mail: ganzheng@essex.ac.uk).

G. K. Karagiannidis is with Aristotle University of Thessaloniki, Thessaloniki 54124, Greece, and also with Khalifa University, Abu Dhabi, United Arab Emirates (e-mail: geokarag@ieee.org).

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier 10.1109/LSP.2015.2428812

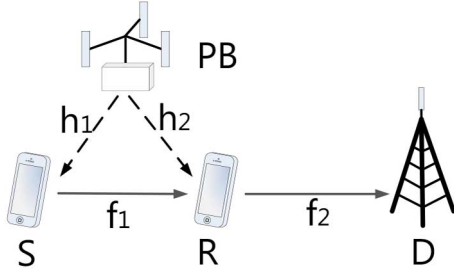


Fig. 1. System model.

is the identity matrix of appropriate size.  $\Pi_{\mathbf{X}} = \mathbf{X}(\mathbf{X}^\dagger \mathbf{X})^{-1} \mathbf{X}^\dagger$  is the orthogonal projection onto the column space of  $\mathbf{X}$ , and  $\Pi_{\mathbf{X}}^\perp = \mathbf{I} - \Pi_{\mathbf{X}}$  is the orthogonal projection onto the orthogonal complement of the column space of  $\mathbf{X}$ .

## II. SYSTEM MODEL

We consider a communication system where the source S communicates with destination D with the assistance of the relay R, as depicted in Fig. 1. We assume that both S and R are energy constrained, hence rely on the external energy charging via wireless power transfer from a dedicated PB. All three communication nodes are equipped with a single antenna, while the PB is equipped with  $N$  antennas. Full channel state information (CSI) of the PB and source and relay links is assumed at the PB. In practice, the channel can be estimated by overhearing the pilot send by the source and relay. In addition, the channel magnitudes of the two hop information links are assumed to be known at the PB, which, for instance, could be obtained through feedback from the relay.

The entire communication consists of two different phases, namely, *energy harvesting* and *information transmission*. Assuming a block time of  $T$ , during the first phase of duration  $\tau T$ , where  $0 < \tau < 1$ , S and R harvest energy from the PB. The remaining time of duration  $(1 - \tau)T$  is equally partitioned into two parts, during the first half period, S transmits information to R and during the second half, R forwards the information to D.

During the energy harvesting phase, the received signal at S and R can be expressed, respectively, as

$$y_s^e = \sqrt{P d_1^{-\alpha}} \mathbf{h}_1^T \mathbf{x}_e + n_s \quad \text{and} \quad y_r^e = \sqrt{P d_2^{-\alpha}} \mathbf{h}_2^T \mathbf{x}_e + n_r,$$

where  $P$  is the transmit power at the PB,  $d_1$  and  $d_2$  denote the distances between PB and S, PB and R, respectively. Furthermore,  $\alpha$  is the path loss exponent,  $\mathbf{h}_1$  and  $\mathbf{h}_2$  are the channel vectors of size  $N \times 1$ ,  $\mathbf{x}_e$  is an  $N \times 1$  vector satisfying  $E\{\mathbf{x}_e^\dagger \mathbf{x}_e\} = 1$ , and  $n_s$  and  $n_r$  are the zero-mean additive white Gaussian noise (AWGN) samples with variance  $N_0$ .

Since the PB is equipped with multiple antennas, energy beamforming could be applied to improve the efficiency of energy transfer, i.e.,  $\mathbf{x}_e = \mathbf{w} s_e$ , where  $\mathbf{w}$  is the beamforming vector with  $\|\mathbf{w}\|^2 = 1$ , while  $s_e$  is the energy symbol with unit

power. As such, the total received energy at the S and R at the end of the first phase can be expressed as

$$E_s = \eta |\mathbf{w}^T \mathbf{h}_1|^2 P \tau T d_1^{-\alpha}, \quad (1)$$

and

$$E_r = \eta |\mathbf{w}^T \mathbf{h}_2|^2 P \tau T d_2^{-\alpha}, \quad (2)$$

respectively, where  $0 < \eta < 1$  is the energy conversion efficiency.

In the first half of the second phase, S transmits information to R using the energy harvested in the first phase. Hence, the received signal  $y_r$  at R is given by

$$y_r = \sqrt{\frac{2E_s}{(1 - \tau)T d_3^\alpha}} f_1 s_0 + n_r, \quad (3)$$

where  $d_3$  denotes the distance between S and R,  $f_1$  is the channel coefficient,  $s_0$  is the information symbol with unit energy.

Upon receiving the source signal, the relay first decodes the source symbol and then forwards it to the destination using the energy harvested during the first phase.<sup>1</sup> As such the signal at D can be expressed as

$$y_d = \sqrt{\frac{2E_r}{(1 - \tau)T d_4^\alpha}} f_2 s_r + n_d, \quad (4)$$

where  $d_4$  denotes the distance between R and D,  $f_2$  is the channel coefficient,  $s_r$  is the relay signal with unit energy, and  $n_d$  is a sample of the AWGN with variance  $N_0$ .

Therefore, the effective end-to-end SNR at the destination can be written as

$$\gamma = \frac{2\tau\eta P}{(1 - \tau)N_0} \min \left\{ \frac{|\mathbf{w}^T \mathbf{h}_1|^2 |f_1|^2}{d_1^\alpha d_3^\alpha}, \frac{|\mathbf{w}^T \mathbf{h}_2|^2 |f_2|^2}{d_2^\alpha d_4^\alpha} \right\}. \quad (5)$$

## III. THROUGHPUT OPTIMIZATION

The achievable system's throughput,  $R$ , can be expressed as (6), shown at the bottom of the page. Hence, the following optimization problem is created:

$$\mathcal{P}1: \quad \max_{\tau, \mathbf{w}} \quad R \quad (7)$$

$$\text{s.t.} \quad 0 < \tau < 1 \quad (8)$$

$$\|\mathbf{w}\|^2 = 1. \quad (9)$$

At the first glance, the above problem requires the joint optimization of  $\tau$  and  $\mathbf{w}$ , which is in general a difficult task. Nevertheless, a close observation reveals that the special structure of  $\mathcal{P}1$  allows for a separate optimization of  $\tau$  and  $\mathbf{w}$ . Specifically, we present the following key result.

<sup>1</sup>Please note, we have ignored the processing power required by the transmit/receive circuitry at the relay as in [7], [11], [20]. This assumption is justifiable since the transmission energy is the dominant source of energy consumption.

$$R = \frac{(1 - \tau)}{2} \times \log_2 \left( 1 + \frac{2\tau\eta P}{(1 - \tau)N_0} \min \left\{ \frac{|\mathbf{w}^T \mathbf{h}_1|^2 |f_1|^2}{d_1^\alpha d_3^\alpha}, \frac{|\mathbf{w}^T \mathbf{h}_2|^2 |f_2|^2}{d_2^\alpha d_4^\alpha} \right\} \right). \quad (6)$$

*Proposition 1:* The original optimization problem,  $\mathcal{P}1$ , is equivalent to the following:

$$\mathcal{P}2: \max_{\tau} \frac{(1-\tau)}{2} \log_2 \left( 1 + \frac{2\tau\eta P}{(1-\tau)N_0} z_m \right) \quad (10)$$

$$\text{s.t. } 0 < \tau < 1, \quad (11)$$

where  $z_m$  is defined as

$$z_m = \min \left\{ \frac{|\hat{\mathbf{w}}^T \mathbf{h}_1|^2 |f_1|^2}{d_1^\alpha d_3^\alpha}, \frac{|\hat{\mathbf{w}}^T \mathbf{h}_2|^2 |f_2|^2}{d_2^\alpha d_4^\alpha} \right\}, \quad (12)$$

with  $\hat{\mathbf{w}}$  being the solution of the following optimization problem:

$$\mathcal{P}3: \max_{\mathbf{w}} \min \left\{ \frac{|\mathbf{w}^T \mathbf{h}_1|^2 |f_1|^2}{d_1^\alpha d_3^\alpha}, \frac{|\mathbf{w}^T \mathbf{h}_2|^2 |f_2|^2}{d_2^\alpha d_4^\alpha} \right\} \quad (13)$$

$$\text{s.t. } \|\mathbf{w}\|^2 = 1. \quad (14)$$

*Proof:* Define function  $g(\tau, z)$  as

$$g(\tau, z) = \frac{(1-\tau)}{2} \log_2 \left( 1 + \frac{2\tau\eta P}{(1-\tau)N_0} z \right), \quad (15)$$

where  $0 < \tau < 1$  and  $z$  is a positive real number. It is easy to prove that function  $g(\tau, z)$  is an increasing function with respect to  $z$ . Now consider two positive real numbers  $z_1$  and  $z_2$  such that  $z_2 > z_1$ , and let  $\tau_i$  being the value of  $\tau$  which maximizes  $g(\tau, z_i)$ , i.e.,  $g(\tau_i, z_i) \geq g(\tau, z_i)$  for all  $\tau$ ,  $i = 1, 2$ . Then, it holds that

$$g(\tau_2, z_2) \geq g(\tau_1, z_2) \geq g(\tau_1, z_1), \quad (16)$$

which indicates that the maximum of  $g(\tau, z)$  is achieved at the point when  $z$  attains its maximum. Therefore, a sequential optimization of problems  $\mathcal{P}3$  and  $\mathcal{P}2$  yields the optimal solution for the original problem  $\mathcal{P}1$ . ■

In the following, we investigate the optimal solutions for the problems  $\mathcal{P}2$  and  $\mathcal{P}3$ .

*Proposition 2:* The optimal  $\tau$  for the optimization problem  $\mathcal{P}2$  is given by

$$\hat{\tau} = \frac{e^{W(\frac{\beta-1}{e})+1} - 1}{\beta + e^{W(\frac{\beta-1}{e})+1} - 1}, \quad (17)$$

where  $W(x)$  is the Lambert W function [21], and  $\beta = \frac{2\eta P z_m}{N_0}$ .

*Proof:* The proof follows from the results presented in [15, Appendix A]. ■

We now turn to problem  $\mathcal{P}3$ , and we have the following key result:

*Theorem 1:* The optimal beamforming vector  $\hat{\mathbf{w}}$  for the optimization problem  $\mathcal{P}3$  can be expressed as

$$\hat{\mathbf{w}} = \bar{x} \frac{\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1^*}{\|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|} + \sqrt{1-\bar{x}^2} \frac{\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1^*}{\|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|}, \quad (18)$$

where  $\hat{\mathbf{h}}_1 = \frac{|f_1|}{\sqrt{d_1^\alpha d_3^\alpha}} \mathbf{h}_1$ ,  $\hat{\mathbf{h}}_2 = \frac{|f_2|}{\sqrt{d_2^\alpha d_4^\alpha}} \mathbf{h}_2$ ,  $a = \|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|$ ,  $b =$

$$\|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|, \text{ and } c = \frac{|\hat{\mathbf{h}}_1^T \Pi_{\hat{\mathbf{h}}_2} \hat{\mathbf{h}}_2|}{\|\Pi_{\hat{\mathbf{h}}_2} \hat{\mathbf{h}}_1\|}, \text{ and } \bar{x} \text{ being}$$

$$\bar{x} = \begin{cases} \frac{a}{\sqrt{a^2+b^2}}, & c \geq \frac{a^2+b^2}{a}, \\ \frac{b}{\sqrt{(a-c)^2+b^2}}, & a \leq c < \frac{a^2+b^2}{a}, \\ 1, & c < a. \end{cases} \quad (19)$$

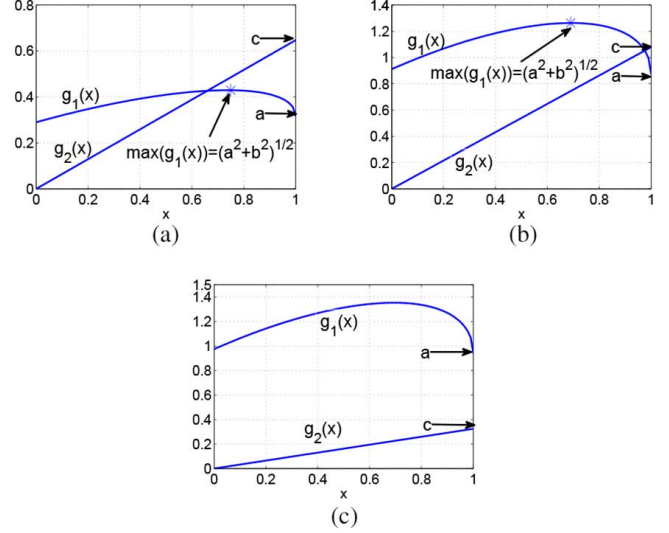


Fig. 2. Three different cases for the maximization of  $g(x)$  (a) Case 1 (b) Case 2 (c) Case 3.

*Proof:* According to [22, Corollary 1], the optimal beamforming vector  $\hat{\mathbf{w}}$  can be expressed as

$$\hat{\mathbf{w}} = x \frac{\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1^*}{\|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|} + \sqrt{1-x^2} \frac{\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1^*}{\|\Pi_{\hat{\mathbf{h}}_2}^\perp \hat{\mathbf{h}}_1\|}, \quad (20)$$

where  $x \in [0, 1]$ . Now let us define  $g_1(x) \triangleq |\hat{\mathbf{w}}^T \hat{\mathbf{h}}_1| = ax + b\sqrt{1-x^2}$ , and  $g_2(x) \triangleq |\hat{\mathbf{w}}^T \hat{\mathbf{h}}_2| = cx$ . Then, the original optimization problem  $\mathcal{P}1$  is equivalent to maximize the function  $g(x)$ , i.e.,

$$\max_x g(x), \quad \text{s.t. } 0 \leq x \leq 1, \quad (21)$$

where  $g(x)$  is defined as

$$g(x) \triangleq \min(g_1(x), g_2(x)) = \min(ax + b\sqrt{1-x^2}, cx).$$

It is easy to show that  $g_1(x)$  is a concave function with respect to  $x$ , hence, its maximum can be attained by solving  $g_1'(\hat{x}) = 0$ , which gives  $\hat{x} = \frac{a}{\sqrt{a^2+b^2}}$ , and  $g_1(\hat{x}) = \sqrt{a^2+b^2}$ .

Now, as shown in Fig. 2, there are three different scenarios:

- Case 1: It can be easily observed that the  $x$ -label of the cross point of  $g_1(x)$  and  $g_2(x)$ , i.e.,  $x_c$ , can be characterized by  $g_1(x_c) = g_2(x_c)$ , which gives  $x_c = \frac{b}{\sqrt{b^2+(c-a)^2}}$ .

If the slope of  $g_2(x)$  is sufficiently large, such that the cross point appears before  $g_1(x)$  attaining its maximum, i.e.,  $x_c \leq \hat{x}$ , which gives  $c \geq \frac{a^2+b^2}{a}$ , then, the maximum of  $g(x)$  is achieved at  $\bar{x} = \hat{x} = \frac{a}{\sqrt{a^2+b^2}}$ , which is also the maximum point of  $g_1(x)$ , as shown in Fig. 2(a).

- Case 2: The cross point appears after  $g_1(x)$  attaining its maximum, i.e.,  $a \leq c < \frac{a^2+b^2}{a}$ , then, the maximum of  $g(x)$  is achieved at the cross point, i.e.,  $\bar{x} = x_c = \frac{b}{\sqrt{(a-c)^2+b^2}}$ , as shown in Fig. 2(b).

- Case 3: There is no cross point between  $g_1(x)$  and  $g_2(x)$ , i.e.,  $g_1(x) \geq g_2(x)$  for all  $x$ , namely,  $c < a$ , then, the maximum of  $g(x)$  is identical to the maximum of  $g_2(x)$  which is achieved at the point  $\bar{x} = 1$ , as shown in Fig. 2(c). ■

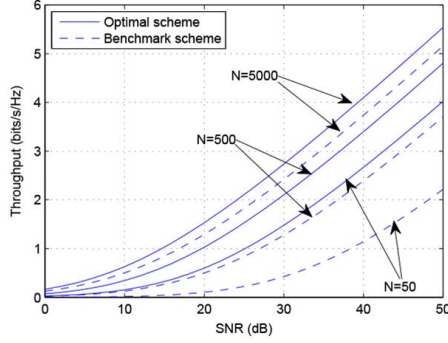


Fig. 3. Throughput comparison between the optimal scheme and benchmark scheme for different  $N$ .

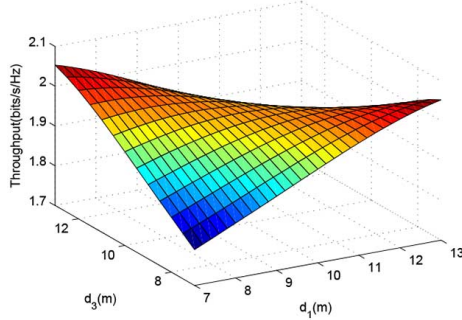


Fig. 4. Impact of node positions on the system throughput.

#### IV. NUMERICAL RESULTS AND DISCUSSION

In this section, numerical and simulations results are presented to illustrate the impact of key system parameters on the system's throughput. Without loss of generality, we set the energy conversion efficiency  $\eta = 0.4$ , and path-loss exponent  $\alpha = 3$ . Please note, the throughput is obtained by averaging over  $10^3$  independent channel realizations.

To demonstrate the superiority of the proposed optimal scheme, we compare it with an intuitive benchmark scheme by looking into the asymptotic large antenna regime, where the optimal beamforming vector becomes

$$\bar{\mathbf{w}} = \left( \frac{|f_2|}{\sqrt{d_2^\alpha d_4^\alpha}} \frac{\mathbf{h}_1^*}{\|\mathbf{h}_1\|} + \frac{|f_1|}{\sqrt{d_1^\alpha d_3^\alpha}} \frac{\mathbf{h}_2^*}{\|\mathbf{h}_2\|} \right) / \sqrt{\frac{|f_2|^2}{d_2^\alpha d_4^\alpha} + \frac{|f_1|^2}{d_1^\alpha d_3^\alpha}}. \quad (22)$$

The rationale behind the choice of  $\bar{\mathbf{w}}$  is that, the optimal beamforming vector should be a linear combination of  $\mathbf{h}_1^*$  and  $\mathbf{h}_2^*$ , hence, the key is to design the optimal weights. Capitalizing on the asymptotical orthogonality of  $\mathbf{h}_1^*$  and  $\mathbf{h}_2^*$  when  $N \rightarrow \infty$ , the optimal weights can be easily obtained.

Fig. 3 depicts the achievable throughput of the optimal scheme and the benchmark scheme with  $d_1 = d_2 = 3$  m and  $d_3 = d_4 = 5$  m. It can be easily observed that the optimal scheme outperforms the benchmark scheme, and the performance gap is rather significant for moderate number of antennas  $N$ . On the other hand, when  $N$  is sufficiently large, i.e.,  $N = 5000$ , the performance gap narrows substantially. This is expected since the benchmark scheme becomes asymptotically optimal. We can also observe that the throughput improves, when  $N$  increases, which is also intuitive since the energy transfer efficiency improves with a large size of antenna array.

Fig. 4 examines the impact of node positions on the throughput performance when  $N = 10$ ,  $d_1 + d_2 = 20$  m, and  $d_3 + d_4 = 20$  m, as a function of  $d_1$  and  $d_3$ , both vary from

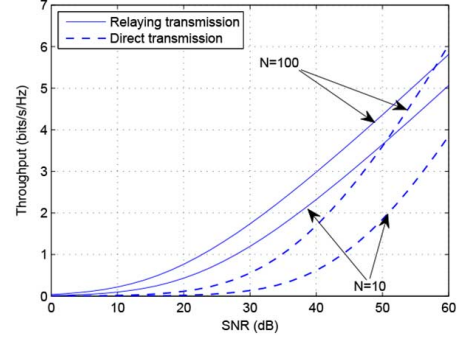


Fig. 5. Throughput comparison: Relaying v.s. Direct transmission.

7 to 13. It can be observed that higher throughput is attained at the point  $d_1 = 7$  and  $d_3 = 13$ , a scenario where the PB is close to the source, while the relay is close to the destination; or at the point  $d_1 = 13$  and  $d_3 = 7$ , a scenario where the PB is close to the relay, while the relay is close to the source. The above results are somehow intuitive, since the performance of dual-hop relaying systems is bottlenecked by the weakest link, hence, an optimized system shall achieve a fine balance between the two hops.

Another interesting observation from Fig. 4 is that the symmetric setup, i.e., the point  $d_1 = d_2 = 10$  and  $d_3 = d_4 = 10$ , does not yield the maximum throughput. This is in sharp contrast to the conventional dual-hop relaying systems, where it is always desirable to put the relay node in the middle of the source and destination link. The reason is that, with the introduction of PB, in addition to the distance of the information transfer links, the throughput performance also heavily depends on the distance of the energy transfer links. As a matter of fact, the throughput is determined by  $d_1^\alpha d_3^\alpha$ , as shown in the end-to-end SNR expression (5). Since  $(7 \times 13)^\alpha < (10 \times 10)^\alpha$ , it becomes obvious why the maximum throughput is achieved at point  $d_1 = 3$  and  $d_3 = 13$ .

Fig. 5 compares the achievable throughput of the dual-hop relaying system with that of direct transmission system with optimized time split and beamforming vector. As can be readily observed, at SNR levels of practical interest, i.e.,  $0 \text{ dB} < \text{SNR} < 50 \text{ dB}$ , adopting the relaying structure improves the system throughput. Moreover, the performance gap is more substantial with moderate number of antennas, i.e.,  $N = 10$ . Only if the transmit SNR is very high, direct transmission becomes preferred. This is rather intuitive since at the high SNR regime, the system is degree-of-freedom limited, as such the half-duplex relay operation becomes the bottleneck as manifested through the  $1/2$  factor in the throughput expression. Since in the wirelessly powered communications systems, the source is likely to operate in the power-limited regime, adopting the relaying structure is beneficial in general.

#### V. CONCLUSION

We have optimized the throughput of a relay-assisted wirelessly powered communication system. Specifically, we obtained simple closed-form solutions for the PB energy beamforming vector as well as the optimal time split for the energy harvesting phase and information transmission phase. It was shown that the optimal solution yields significant performance gain compared to the intuitive benchmark scheme.

## REFERENCES

- [1] B. Medepally and N. B. Mehta, "Voluntary energy harvesting relays and selection in cooperative wireless networks," *IEEE Trans. Wireless Commun.*, vol. 9, no. 11, pp. 3543–3553, Nov. 2010.
- [2] W. Lumpkins, "Nikola Tesla's dream realized: Wireless power energy harvesting," *IEEE Consumer Electron. Mag.*, vol. 3, no. 1, pp. 39–42, Jan. 2014.
- [3] L. R. Varshney, "Transporting information and energy simultaneously," in *Proc. IEEE ISIT 2008*, Toronto, Canada, Jul. 2008, pp. 1612–1616.
- [4] P. Grover and A. Sahai, "Shannon meets Tesla: Wireless information and power transfer," in *Proc. IEEE ISIT 2010*, Austin, TX, Jun. 2010, pp. 2363–2367.
- [5] R. Zhang and C. Ho, "MIMO broadcasting for simultaneous wireless information and power transfer," *IEEE Trans. Wireless Commun.*, vol. 12, no. 5, pp. 1989–2001, May 2013.
- [6] L. Liu, R. Zhang, and K. C. Chua, "Wireless information and power transfer: A dynamic power splitting approach," *IEEE Trans. Commun.*, vol. 61, no. 9, pp. 3990–4001, Sep. 2013.
- [7] X. Zhou, R. Zhang, and C. Ho, "Wireless information and power transfer: Architecture design and rate-energy tradeoff," *IEEE Trans. Commun.*, vol. 61, no. 11, pp. 4754–4767, Nov. 2013.
- [8] Z. Xiang and M. Tao, "Robust beamforming for wireless information and power transmission," *IEEE Wireless Commun. Lett.*, vol. 1, no. 4, pp. 372–375, 2012.
- [9] D. W. K. Ng, E. S. Lo, and R. Schober, "Wireless information and power transfer: Energy efficiency optimization in OFDMA systems," *IEEE Trans. Wireless Commun.*, vol. 12, no. 12, pp. 6352–6370, Dec. 2013.
- [10] K. Huang and E. G. Larsson, "Simultaneous information and power transfer for broadband wireless systems," *IEEE Trans. Signal Process.*, vol. 61, no. 23, pp. 5972–5986, 2013.
- [11] A. A. Nasir, X. Zhou, S. Durrani, and R. A. Kennedy, "Relaying protocols for wireless energy harvesting and information processing," *IEEE Trans. Wireless Commun.*, vol. 12, no. 7, pp. 3622–3636, Jul. 2013.
- [12] Z. Ding, S. M. Perlaza, I. Esnaola, and H. V. Poor, "Power allocation strategies in energy harvesting wireless cooperative networks," *IEEE Trans. Wireless Commun.*, vol. 13, no. 2, pp. 846–860, Feb. 2014.
- [13] Z. Ding and H. V. Poor, "Cooperative energy harvesting networks with spatially random users," *IEEE Signal Process. Lett.*, vol. 20, no. 12, pp. 1211–1214, Dec. 2013.
- [14] Z. Ding, I. Krikidis, B. Sharif, and H. V. Poor, "Wireless information and power transfer in cooperative networks with spatially random relays," *IEEE Trans. Wireless Commun.*, vol. 13, no. 8, pp. 4440–4453, Aug. 2014.
- [15] C. Zhong, H. Suraweera, G. Zheng, I. Krikidis, and Z. Zhang, "Wireless information and power transfer with full duplex relaying," *IEEE Trans. Commun.*, vol. 62, no. 10, pp. 3447–3461, Oct. 2014.
- [16] I. Krikidis, S. Sasaki, S. Timotheou, and Z. Ding, "A low complexity antenna switching for joint wireless information and energy transfer in MIMO relay channels," *IEEE Trans. Commun.*, vol. 62, no. 5, pp. 1577–1587, May 2014.
- [17] I. Krikidis, "Simultaneous information and energy transfer in large-scale networks with/without relaying," *IEEE Trans. Commun.*, vol. 62, no. 3, pp. 900–912, Mar. 2014.
- [18] K. Huang and X. Zhou, "Cutting last wires for mobile communication by microwave power transfer," *IEEE Commun. Mag.*, 2014, submitted to.
- [19] K. Huang and V. K. N. Lau, "Enabling wireless power transfer in cellular networks: Architecture, modeling and deployment," *IEEE Trans. Wireless Commun.*, vol. 13, no. 2, pp. 902–912, Feb. 2014.
- [20] B. Medepally and N. B. Mehta, "Voluntary energy harvesting relays and selection in cooperative wireless networks," *IEEE Trans. Wireless Commun.*, vol. 9, no. 11, pp. 3543–3553, Nov. 2010.
- [21] R. Corless, G. Gonnet, D. Hare, D. Jeffrey, and D. Knuth, "On the Lambert W function," in *Advances in Computational Mathematics*. New York, NY, USA: Springer-Verlag, 1996, pp. 329–359.
- [22] E. Jorswieck, E. Larsson, and D. Danev, "Complete characterization of the pareto boundary for the MISO interference channel," *IEEE Trans. Signal Process.*, vol. 56, no. 10, pp. 5292–5296, Oct. 2008.