

# LOW BITRATE INFORMED SOURCE SEPARATION OF REALISTIC MIXTURES

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## ABSTRACT

Demixing consists in recovering the sounds that compose a multichannel mix. Important applications include karaoke or respatialization. Several approaches to this problem have been proposed in a coding/decoding framework, which are denoted either as spatial audio object coding or informed source separation. They assume that the constituent sounds are available at an encoding stage and used to compute a side-information transmitted to the end-user. At a decoding stage, only the mixtures and the side information are used to recover the sources. Here, we propose an advanced model, which encompasses many practical scenarios and permits to reach bitrates as low as 0.5kbps/source. First, the sources may be mono or multichannel. Second, the mixing process is assumed to be diffuse, generalizing the usual linear-instantaneous or convolutive cases and permitting professional mixes to be processed. Third, the signals to be recovered may either be the original sources or their spatial images.

**Index Terms**— audio upmixing, Wiener filtering, spatial audio object coding, informed source separation

## 1. INTRODUCTION

The ability to recover the constituent audio signals from their multichannel mixtures is at the core of many applications of audio signal processing. Among them, we can mention karaoke, which consists in muting one of the instruments, usually the voice signal. Another important application is respatialization, which consists in dynamically modifying the spatial positions of the different audio signals *within* the mixtures. This processing is important in recent entertainment applications such as videogames or 3D-movies, where the positions of the sources constantly vary over time.

A first naive way to achieve such applications is to separately encode all constituent sounds at the coder and transmit them as such to the decoder. In that case, the desired mixtures are automatically constructed at the decoder using the available separated sounds. This strategy faces three major drawbacks. First, it requires a high bitrate. Indeed, the separate encoding of all the audio sources requires bitrates of at least, say, 24kbps/source using recent audio codecs like MPEG4 HE-AAC v2 [3] to be of reasonable quality, leading to high bitrates if the number of sources is important. Second, this strategy does not permit to benefit from a professional mixing. Indeed, providing mixed audio signals of professional quality is difficult and requires expert knowledge, which cannot easily be imitated by an automated process. Finally, transmitting separated signals is often not considered as a viable option by copyrights owners, who are very reluctant to broadcast the separated tracks from famous songs.

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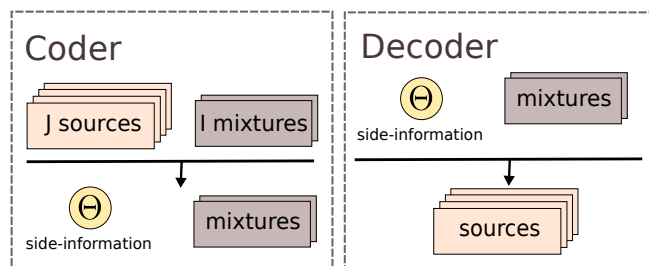


Fig. 1. High-level ISS/SAOC scheme

Hence, much research has focused on how to efficiently encode the constituent sources present in an audio mixture in a coding/decoding framework. At the coder, both the constituent tracks and the mixtures are known and a side-information is produced. At the decoder, only the mixtures and the side information are processed to recover the sources. In the literature, this problem has been independently addressed by two distinct communities. First, Spatial Audio Object Coding (SAOC, [11, 5, 6]) techniques have been proposed to recover separated audio *objects*, extending classical Spatial Audio Coding methods (SAC [10, 1]), whose purpose is to obtain a good respatialization of some transmitted *downmix*. Independently from SAOC, researchers from the source separation community have addressed the same exact problem using sophisticated source separation techniques [20, 17, 15, 18]. The resulting methods are commonly referred to as *Informed Source Separation* (ISS) in this community. Interestingly enough, bridges between source separation and audio coding have recently emerged [22] and theoretical analysis of ISS in terms of source coding have been proposed in [19, 16].

Both SAOC and ISS share the same general framework depicted in figure 1 : the signals to be recovered at the decoder are only observed through a *downmix*. The operations performed to obtain the original signals vary from one technique to the other, but the common strategy of all those techniques is to assume that the sources can be efficiently recovered through a *filtering* of the mixtures. While some methods [20] perform a local inversion of the mixing process in the time-frequency domain, others make use of an optimal filtering strategy [6, 5, 18, 15]. The mixing process to be inverted is either modeled as linear instantaneous [11, 5, 21, 20, 18] or convolutive [17, 15]. In any case, the side-information which is transmitted from the coder to the decoder usually consists of the optimal parameters to be used for the filtering.

Existing informed separation methods exhibit several common drawbacks. First, they are restrictive with respect to the mixing process considered. Most of them rely on the assumptions that the observed mixtures are either linear instantaneous or convolutive and that the mixing parameters are known. These assumptions prevent the processing of real professional mixtures, which may exhibit some non-linearities or some spatial spreading of the sources, due to

the use of advanced audio effects. A second restriction of existing ISS methods is that they either focus on the recovery of the original mono sources [20, 15, 9] (hence permitting high-quality respatialization) or on the mere separation of source images [13, 17], which is sufficient for karaoke applications. To the best of our knowledge, there is no available ISS method that can handle both cases in a principled way. Concerning SAOC, it can benefit from important advances made in audio coding to efficiently account for spatial images [3]. Still, we are not aware of a study which merges SAOC decoding with advanced spatial rendering. Finally, there is no available ISS method that can efficiently cope with multichannel sources : all techniques assume that the sources are mono signals, which may not be true in the case of music production (think of the output of a synthesizer).

In this paper, we propose a general Gaussian framework to address all these issues. The sources are modelled as locally stationary Gaussian processes and the mixing process is assumed diffuse — or full-rank — as recently introduced in [4]. In this framework, the sources can be observed at the coder either as mono or multichannel, and can be recovered at the decoder either as observed at the coder or as images, i.e. as they appear within the mixtures. The parameters of this model can be encoded very efficiently through a Nonnegative Tensor Factorization [17, 18] or through image compression algorithms [17]. Resulting bitrates can be as low as 0.5kbps/source, for perceptually good separation quality.

This paper is organized as follows. First, we present the notation and models in section 2. Then, we detail all the algorithms required by the corresponding coding/decoding framework in section 3. Finally, we provide some experimental results in section 4 which demonstrate the efficiency of the approach and we conclude in section 5.

## 2. NOTATION AND MODEL

### 2.1. Notation

At the coder, the observed signals are the waveforms of the *sources*  $\tilde{\mathbf{s}}$  and the *mixtures*  $\tilde{\mathbf{x}}$ . We assume that there are  $J$  sources and  $I$  mixtures to consider. A typical case is  $I = 2$  for stereo mixtures. All waveforms are assumed to be of the same length  $L$ .

Some of the sources may be observed as mono sources. Let  $\mathcal{S}_p \subset \mathbb{N}_J$  be the indices of those sources<sup>1</sup> and let  $\mathcal{S}_d = \mathbb{N}_J \setminus \mathcal{S}_p$  be the indices of the sources which are observed as multichannel signals. We assume for simplicity that all multichannel sources have  $I$  channels, just like the mixtures (e.g. stereo sources for stereo mixtures). Let  $\tilde{\mathbf{s}}(\cdot, \cdot, j)$  denote the observed waveforms for source  $j$ . Its dimension is either  $L \times 1$  if  $j \in \mathcal{S}_p$ , noting  $\tilde{\mathbf{s}}(t, j)$  in that case, or  $L \times I$  if  $j \in \mathcal{S}_d$ , hence noting  $\tilde{\mathbf{s}}(t, i, j)$ . Similarly, let  $\tilde{\mathbf{x}}(t, i)$  be the observed value of the mixture  $i$  at time  $t$ .

Whereas an observed source  $\tilde{\mathbf{s}}(\cdot, \cdot, j)$  may be mono or multichannel, its *spatial image*  $\tilde{\mathbf{y}}(\cdot, \cdot, j)$  within the mixtures necessarily has  $I$  channels. The spatial image of a source is defined as how it appears *within* the mixtures. For example, if a stereophonic mixture is built from three monophonic sources such as voice, bass and piano, it is not the monophonic sum of these sources which is observed but the sum of their *spatial images* :

$$\forall (t, i), \tilde{\mathbf{x}}(t, i) = \sum_{j=1}^J \tilde{\mathbf{y}}(t, i, j).$$

1.  $\mathbb{N}_J = [1, \dots, J]$  is the set comprising the  $J$  first strictly positive integers.

This notation being given, we will not process the signals in the time domain, but rather in a Time-Frequency representation. In this paper, we will consider the Short-Term Fourier Transform (STFT), which consists in splitting each signal considered into small overlapping frames before applying a Fourier transform on each of them. The resulting STFTs will be denoted without the tilde notation. Hence :

- $\mathbf{s}(f, n, \cdot, j)$  denotes the — complex — observed values of the STFTs of source  $j$  at Time-Frequency (TF) bin  $(f, n)$ . If  $j \in \mathcal{S}_p$ , it is a complex single  $(1 \times 1)$  value, because that source is monophonic. If  $j \in \mathcal{S}_d$ , it is a  $I \times 1$  vector, because that source is multichannel.
- $\mathbf{x}(f, n, \cdot) = [\mathbf{x}(f, n, 1), \dots, \mathbf{x}(f, n, I)]^\top$  is the  $I \times 1$  vector gathering the  $I$  coefficients of the STFTs of the mixtures at TF bin  $(f, n)$ . Notation  $\cdot^\top$  denotes transposition.
- $\mathbf{y}(f, n, \cdot, j) = [\mathbf{y}(f, n, 1, j), \dots, \mathbf{y}(f, n, I, j)]^\top$  is the  $I \times 1$  vector gathering the  $I$  coefficients of the STFTs of the image of source  $j$  into the mixtures at TF bin  $(f, n)$ .

Waveforms can be efficiently recovered through overlap-add procedures. All STFTs are assumed to have the same number  $F$  of frequency bins and the same number  $N$  of frames.

### 2.2. Models

#### 2.2.1. Sources model

In the STFT domain and for each source  $j$ , the observed signal  $\mathbf{s}(f, n, \cdot, j)$  is supposed to be the outcome of an underlying stochastic process  $s(f, n, \cdot, j)$ . In this study, we will simply assume that all non redundant TF bins  $(f, n)$  are independent and Gaussian. As we have demonstrated in [14], this assumption amounts to consider that all the frames are independent and that within each frame, the signals are stationary and Gaussian, which is often a good approximation for audio signals. Skipping the details that will be presented in a longer study, the model amounts to assuming that :

$$\forall j \in \mathcal{S}_p \quad \mathbf{s}(f, n, j) \sim \mathcal{N}_c(0, P(f, n, j)) \quad (1)$$

$$\forall j \in \mathcal{S}_d \quad \mathbf{s}(f, n, \cdot, j) \sim \mathcal{N}_c\left(0, P(f, n, j) R^{obs}(f, j)\right), \quad (2)$$

where :

- $P(f, n, j) \geq 0$  is the power of source  $j$  at bin  $(f, n)$ . It is a nonnegative quantity.
- $\mathcal{N}_c(\mathbf{z} | 0, \sigma^2) = \frac{1}{\pi \sigma^2} \exp\left(-\frac{|\mathbf{z}|^2}{\sigma^2}\right)$  is the complex circular centered Gaussian distribution of variance  $\sigma^2$ .
- For multichannel sources,  $R^{obs}(f, j)$  is a  $I \times I$  positive definite *observation spatial covariance matrix*.

Equation (1) simply means that the STFT coefficients for one given mono source  $j \in \mathcal{S}_p$  are independent and distributed with respect to a complex and centered Gaussian distribution, whose variance is the power of the source at that bin.

In the case of multichannel sources ( $j \in \mathcal{S}_d$ ), we assume through equation (2) that the different channels of a source signal at TF bin  $(f, n)$  are Gaussian and correlated. This model is reminiscent of the work by DUONG et al. in [4]. Basically, the covariance is given by the  $R^{obs}(f, j)$  matrix and scaled according to  $P(f, n, j)$ .

Since  $P(f, n, j)$  are to be transmitted from the coder to the decoder, it is important to reduce the corresponding number of coefficients. As in [17], we propose two techniques to approximate  $P(f, n, j)$ . The first one is a Nonnegative Tensor Factorization model (NTF) :

$$\hat{P}(f, n, j) = \sum_{k=1}^K W_{fk} H_{nk} Q_{jk} \quad (3)$$

where  $K \in \mathbb{N}$  is called *the number of components* and where  $W$ ,  $H$  and  $Q$  are  $F \times K$ ,  $N \times K$  and  $J \times K$  nonnegative matrices, respectively. The main feature of this model in our context is to reduce the number of parameters required to encode  $P$  from  $FNJ$  to  $(F + N + J)K$ . The second source model we propose is based on image compression techniques such as JPEG [23]. Since  $P(f, n, j)$  is a nonnegative quantity,  $P$  can be seen as a set of  $J$  images  $P(\cdot, \cdot, j)$  of dimension  $F \times N$  that can be compressed using dedicated techniques. The learning of the model parameters will be detailed in section 3.

### 2.2.2. Mixing model

Following the work by DUONG *et al.* in [4], we adopt the *diffuse* mixing model (also called *full-rank* in the literature) to account for the relation between the sources and their images. This model generalizes both the linear instantaneous and the convolutive mixing models and notably permits to account for a *stochastic* dependence between the sources and their images instead of the deterministic relationship assumed by convolutive or instantaneous mixing. It is characterized by :

$$\forall j, \mathbf{y}(f, n, \cdot, j) \sim \mathcal{N}_c \left( 0, \hat{P}(f, n, j) R(f, j) \right), \quad (4)$$

where  $R(f, j)$  is the *image spatial covariance matrix* of source  $j$  at frequency band  $f$ . It is a  $I \times I$  positive definite matrix that encodes the covariances between the different channels of the *image* of source  $j$  at frequency  $f$ . Whereas convolutive or instantaneous mixing boils down to assuming a rank-1 image spatial covariance matrix, this general formulation permits to model sources that have a spatial spread, hence the “diffuse” adjective. Spatial covariance matrices  $R(j)$  which are constant throughout the frequency indices as in [7] are possible. This further assumption permits to strongly reduce the number of mixing parameters from  $FI^2J$  to  $I^2J$ .

## 3. ALGORITHMS

### 3.1. Coder

The first task at the coding side is to provide a good estimate for the powers  $P$  of the sources. Here, we consider both the NTF model (3) and Image Compression methods (IC). To this purpose, we propose to first estimate the real powers  $P(f, n, j)$  of the sources and then to approximate them using either NTF or IC.

Concerning mono sources, their powers are easily estimated through maximum likelihood by the power spectrograms of the observations :

$$\forall j \in \mathcal{S}_p, P(f, n, j) = |\mathbf{s}(f, n, j)|^2.$$

Concerning multichannel sources, their powers  $P$  are not so easily derived. However, if  $R^{obs}(f, j)$  is available,  $P(f, n, j)$  can be estimated from  $\mathbf{s}(f, n, \cdot, j)$ . Conversely,  $R^{obs}(f, j)$  can be estimated if all  $P(f, n, j)$  are available. This suggests an iterative procedure which is summarized in Algorithm 1. In practice, only a few iterations are sufficient and a regularization is needed in step 1 to handle silent sources.

When all the  $P(f, n, j)$  are estimated, the parameters for the NTF model are estimated using the classical Algorithm 2 [2, 8, 17] which minimizes the Itakura-Saito divergence between  $P$  and the model  $\hat{P}$  (3)<sup>2</sup>. Once the NTF parameters have been learned, it can

2. Exponentiation is understood element-wise,  $a \cdot b$  and  $\frac{a}{b}$  denote element-wise multiplication and division. If  $v$  is a vector,  $\text{diag} v$  denotes the diagonal matrix whose diagonal is  $v$ . If  $v$  is a matrix, it denotes its diagonal.

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#### Algorithm 1 Estimation of $P(f, n, j)$ for multichannel sources.

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– Input : STFT  $\mathbf{s}(f, n, i, j)$  of multichannel source  $j \in \mathcal{S}_d$ ,  $F \times N \times I$  tensor

– Initialization : set  $P(f, n, j) = \frac{1}{I} \sum_{i=1}^I |\mathbf{s}(f, n, i, j)|^2$

**Repeat :**

1. for each  $f$ ,  $R^{obs}(f, j) \leftarrow \frac{1}{N} \sum_{n=1}^N \frac{\mathbf{s}(f, n, \cdot, j) \mathbf{s}(f, n, \cdot, j)^H}{P(f, n, j)}$
  2. for each  $(f, n)$ ,  
 $P(f, n, j) \leftarrow \frac{1}{I} \mathbf{s}(f, n, \cdot, j)^H R^{obs}(f, j)^{-1} \mathbf{s}(f, n, \cdot, j)$
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#### Algorithm 2 Learning the NTF model from $P$ by minimization of the Itakura-Saito divergence between $\hat{P}$ and $P$ .

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– Inputs :  $P(f, n, j)$ ,  $F \times N \times J$  tensor and  $K \in \mathbb{N}$

– Initialization : set  $W$ ,  $H$  and  $Q$  as random  $F \times K$ ,  $N \times K$  and  $J \times K$  nonnegative matrices.

**Repeat :**

1.  $W \leftarrow W \cdot \frac{\sum_j (\hat{P}(\cdot, \cdot, j)^{-2} \cdot P(\cdot, \cdot, j)) H \text{diag}(Q_{j \cdot})}{\sum_j (\hat{P}(\cdot, \cdot, j)^{-1}) H \text{diag}(Q_{j \cdot})}$
  2.  $H \leftarrow H \cdot \frac{\sum_j (\hat{P}(\cdot, \cdot, j)^{-2} \cdot P(\cdot, \cdot, j))^T w \text{diag}(Q_{j \cdot})}{\sum_j (\hat{P}(\cdot, \cdot, j)^{-2})^T w \text{diag}(Q_{j \cdot})}$
  3.  $\forall j, Q_{j \cdot} \leftarrow \text{diag} \left( \text{diag}(Q_{j \cdot}) \cdot \frac{W^T (\hat{P}(\cdot, \cdot, j)^{-2} \cdot P(\cdot, \cdot, j)) H}{W^T (\hat{P}(\cdot, \cdot, j)^{-1}) H} \right)$
- 

be shown [19] that an efficient way to encode them is first to use a logarithmic compressor followed by uniform quantization of  $\log W$ ,  $\log H$  and  $\log Q$  and entropy coding. The main parameter to control the bitrate in the NTF model is thus the number  $K$  of components.

In the Image Compression (IC) model, encoding is simply achieved as in [17] by applying an image compression algorithm such as JPEG [23] on all  $\{\log P(\cdot, \cdot, j)\}_j$ . The bitrate in the case of IC is thus controlled by the quality parameter of the image compression algorithm considered.

The second task at the coding side is to provide good estimates for the mixing parameters  $R(f, j)$ <sup>3</sup>. Those parameters can be learned efficiently through the Expectation-Maximization Algorithm 3, already presented in [4], with the noticeable difference that  $\hat{P}$  are assumed known and fixed here, which leads in practice to fast convergence. Only a few iterations of Algorithm 3 are usually sufficient. If computational efficiency at the decoder is not an issue, one can note that Algorithm 3 can actually be run at the decoder, since it does not require knowledge of the sources  $\mathbf{s}$ , but only of  $\mathbf{x}$  and  $\hat{P}$ . This permits to avoid transmitting  $\hat{R}$ .

### 3.2. Decoder

At the decoder, the side-information is recovered and decoded. This permits to obtain both the model  $\hat{P}(f, n, j)$ , either through (3) for NTF or through image reconstruction for IC and the mixing parameters  $\hat{R}(f, j)$ . When the mixing parameters  $R(f, j)$  have been estimated, the images can be very simply estimated through minimum mean-squared error minimization by WIENER-like filter-

3. In case of a constant spatial covariance matrix  $R(j)$ , these parameters reduce to  $J$  matrices of dimension  $I \times I$ .

**Algorithm 3** Estimation of the mixing parameters  $R(f, j)$  given  $\mathbf{x}$  and  $\hat{P}$ .

– Inputs STFT  $\mathbf{x}(f, n, i)$  of the mixtures, estimated powers  $\hat{P}(f, n, j)$

– Initialization: define all  $R(f, j)$  as diagonal  $I \times I$  matrices

**Repeat:**

– *Expectation step:* for each  $(f, n, j)$ :

1.  $K_{xx} = \sum_{j=1}^J \hat{P}(f, n, j) R(f, j)$
2.  $G_j = \hat{P}(f, n, j) R(f, j) K_{xx}^{-1}$
3.  $\hat{\mathbf{y}}(f, n, \cdot, j) = G_j \mathbf{x}(f, n, \cdot)$
4.  $\hat{K}_{yy}(f, n, j) = \hat{\mathbf{y}}(f, n, \cdot, j) \hat{\mathbf{y}}(f, n, \cdot, j)^H + (I_I - G_j) P(f, n, j) R(f, j)$

– *Maximization step:*

$$\begin{cases} \forall j, R(j) \leftarrow \frac{1}{N F} \sum_{n, f} \frac{\hat{K}_{yy}(f, n, j)}{\hat{P}(f, n, j)} & \text{if } R(f, j) = R(j) \\ \forall (f, j), R(f, j) \leftarrow \frac{1}{N} \sum_{n=1}^N \frac{\hat{K}_{yy}(f, n, j)}{\hat{P}(f, n, j)} & \text{otherwise} \end{cases}$$

ing [4]:

$$\begin{aligned} \hat{\mathbf{y}}(f, n, \cdot, j) = \\ \hat{P}(f, n, j) R(f, j) \left[ \sum_{j'=1}^J \hat{P}(f, n, j') R(f, j') \right]^{-1} \mathbf{x}(f, n, \cdot) \end{aligned} \quad (5)$$

If the original mono sources are to be recovered instead of the images, they can be estimated through a beamforming strategy as:

$$\hat{\mathbf{s}}(f, n, \cdot, j) = U_j(f) \hat{\mathbf{y}}(f, n, \cdot, j)$$

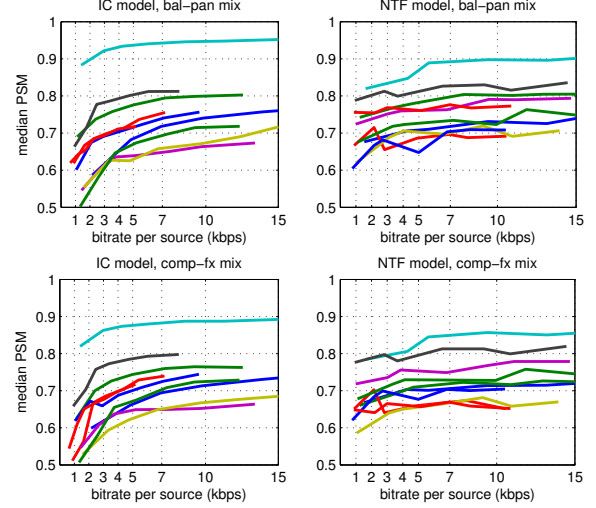
where  $U_j(f)$  is a  $1 \times I$  vector if  $j \in \mathcal{S}_p$  and a  $I \times I$  matrix if  $j \in \mathcal{S}_d$ . Since the coder is able to compute the estimated images (5), it can also compute the  $U_j(f)$  that minimize the mean-squared error between  $U_j(f) \hat{\mathbf{y}}(f, n, \cdot, j)$  and  $\mathbf{s}(f, n, \cdot, j)$  and send it as additional side-information.

#### 4. EVALUATION

We have performed an extensive evaluation of the proposed demixing method on the QUASI database<sup>4</sup>, which is composed of 12 full-length stereo ( $I = 2$ ) songs sampled at 44.1kHz, along with all their constitutive tracks (with an average  $J = 10$ ). For each song, several mixtures are available, as obtained by a professional sound engineer. The simplest mixture consists of a mere panning for the sources (*bal-pan* mix), while the most complex one involves dynamic compressions and audio effects (*comp-fx* mix). For all of the excerpts, we have considered the first minute only and performed an encoding of the sources using both the NTF and the IC models, and we have tested the performance of the method for both the bal-pan and the comp-fx mixes. The metric we used is the Perceptual Similarity Measure (PSM) from PEMO-Q [12], which provides a measure of the perceptual similarity between the original tracks and their estimates. PSM lies between 0 (mediocre) and 1 (identical). Results can be found in figure 2 and some audio examples can be listened to on the webpage dedicated to this paper<sup>5</sup>.

4. [www.tsi.telecom-paristech.fr/aao/?p=605](http://www.tsi.telecom-paristech.fr/aao/?p=605)

5. [www.tsi.telecom-paristech.fr/aao/?p=821](http://www.tsi.telecom-paristech.fr/aao/?p=821)



**Fig. 2.** Perceptual similarity between the original images and their estimates for both the NTF and IC models and different mixing conditions. Each line stands for a different excerpt.

As can be seen on figure 2 and listened to online, the proposed technique for ISS permits to reach good performance at very low bitrates. At 1kbps per source, performance is already remarkably good and sufficient for applications that do not require high fidelity. Perceptual similarity gets higher at 5kbps and artifacts get marginal. The performance of the NTF model at very low bitrates is seen as slightly higher than that of IC, at the cost of a higher computational complexity. Still, informal listening tests seem to favour IC. Finally, both linear instantaneous and professional mixtures are seen to be well supported.

The proposed technique can thus be used for broad audience entertainment applications that require a good quality at low bitrates. For applications that come with a very high-fidelity constraint, parametric ISS as presented here suffers from bounds on achievable performance. This limitation can be overcome using CISS [16, 19], which is based on source coding and is an extension of the ideas presented here, or using an encoding of the residuals as in SAOC [6] or hybrid ISS [22].

#### 5. CONCLUSION

We have proposed a general Gaussian framework for the informed demixing of real-world multichannel mixtures and we have detailed all the corresponding algorithms. The proposed method has several interesting features. First, the source models considered are particularly compact, leading to bitrates as low as 1–10kbps/source. Second, the powerful diffuse model used to account for the mixing process permits to handle realistic professional mixtures as opposed to the classical linear instantaneous or convolutive models. Third, the mixing parameters are estimated automatically at the decoder and need not be transmitted, leading to lower bitrates. Finally, the observed sources at the decoder can be either mono or multichannel and the signals to be recovered at the decoder may be either the signals observed at the coder or their images within the mixtures. Future work will include integrating the proposed model in Coding-based Informed Source Separation, which is compatible with perceptual coding and rate-distortion tradeoffs.

## 6. REFERENCES

- [1] J. Breebaart, S. van de Par, and A. Kohlrausch. High-quality parametric spatial audio coding at low bit rates. In *AES 116th convention*, Berlin, Germany, May 2004.
- [2] A. Cichocki, R. Zdunek, A. H. Phan, and S. Amari. *Nonnegative Matrix and Tensor Factorizations: Applications to Exploratory Multi-way Data Analysis and Blind Source Separation*. Wiley Publishing, September 2009.
- [3] A. C. Den Brinker, J. Breebaart, P. Ekstrand, J. Engdegård, F. Henn, K. Kjörting, W. Oomen, and H. Purnhagen. An overview of the coding standard MPEG-4 audio amendments 1 and 2: HE-AAC, SSC, and HE-AAC v2. *EURASIP J. Audio Speech Music Process.*, 2009:3:1–3:21, January 2009.
- [4] N.Q.K. Duong, E. Vincent, and R. Gribonval. Under-determined reverberant audio source separation using a full-rank spatial covariance model. *Audio, Speech, and Language Processing, IEEE Transactions on*, 18(7):1830–1840, September 2010.
- [5] J. Engdegård, C. Falch, O. Hellmuth, J. Herre, J. Hilpert, A. Hölzer, J. Koppens, H. Mundt, H.O. Oh, H. Purnhagen, B. Resch, L. Terentiev, M.L. Valero, and L. Villemoes. MPEG spatial audio object coding - the ISO/MPEG standard for efficient coding of interactive audio scenes. In *Audio Engineering Society Convention 129*, 11 2010.
- [6] C. Falch, L. Terentiev, and J. Herre. Spatial audio object coding with enhanced audio object separation. In *13th International Conference on Digital Audio Effects (DAFx-10)*, Graz, Austria, September 2010.
- [7] C. Févotte and J.-F. Cardoso. Maximum likelihood approach for blind audio source separation using time-frequency Gaussian models. In *Proc. IEEE Workshop on Applications of Signal Processing to Audio and Acoustics (WASPAA)*, pages 78–81, Mohonk, NY, USA, Oct. 2005.
- [8] C. Févotte and J. Idier. Algorithms for nonnegative matrix factorization with the beta-divergence. *Neural Computation*, 23(9):2421–2456, Sep. 2011.
- [9] S. Gorlow and S. Marchand. Informed source separation: Underdetermined source signal recovery from an instantaneous stereo mixture. In *IEEE Workshop on Applications of Signal Processing to Audio and Acoustics (WASPAA)*, pages 309–312, October 2011.
- [10] J. Herre. From joint stereo to spatial audio coding. In *In Proc. Digital Audio Effects Workshop (DAFx)*, Naples, Italy, October 2004.
- [11] J. Herre and S. Disch. New concepts in parametric coding of spatial audio: From SAC to SAOC. In *IEEE International Conference on Multimedia and Expo (ICME 2007)*, pages 1894–1897, Beijing, China, July 2007.
- [12] R. Huber and B. Kollmeier. PEMO-Q - a new method for objective audio quality assessment using a model of auditory perception. *IEEE Transactions on Audio, Speech, and Language Processing*, 14(6):1902–1911, November 2006.
- [13] A. Liutkus, R. Badeau, and G. Richard. Informed source separation using latent components. In *9th International Conference on Latent Variable Analysis and Signal Separation (LVA/ICA'10)*, St Malo, France, September 2010.
- [14] A. Liutkus, R. Badeau, and G. Richard. Gaussian processes for under-determined source separation. *IEEE Transactions on Signal Processing*, 59(7):3155–3167, July 2011.
- [15] A. Liutkus, S. Gorlow, N. Sturm, S. Zhang, L. Girin, R. Badeau, L. Daudet, S. Marchand, and G. Richard. Informed source separation: a comparative study. In *Proceedings European Signal Processing Conference (EUSIPCO 2012)*, Bucharest, Romania, August 2012.
- [16] A. Liutkus, A. Ozerov, R. Badeau, and G. Richard. Spatial coding-based informed source separation. In *Proceedings European Signal Processing Conference (EUSIPCO 2012)*, Bucharest, Romania, August 2012.
- [17] A. Liutkus, J. Pinel, R. Badeau, L. Girin, and G. Richard. Informed source separation through spectrogram coding and data embedding. *Signal Processing*, 92(8):1937–1949, 2012.
- [18] J. Nikunen, T. Virtanen, and M. Vilermo. Multichannel audio upmixing based on non-negative tensor factorization representation. In *IEEE Workshop Applications of Signal Processing to Audio and Acoustics (WASPAA)*, New Paltz, New York, USA, October 2011.
- [19] A. Ozerov, A. Liutkus, R. Badeau, and G. Richard. Coding-based informed source separation: Nonnegative tensor factorization approach. *IEEE Trans. on Audio, Speech and Language Processing*, 2012. under revision.
- [20] M. Parvaix and L. Girin. Informed source separation of linear instantaneous under-determined audio mixtures by source index embedding. *IEEE Transactions on Audio, Speech, and Language Processing*, 19(6):1721–1733, August 2011.
- [21] M. Parvaix, L. Girin, and J.-M. Brossier. A watermarking-based method for informed source separation of audio signals with a single sensor. *IEEE Transactions on Audio, Speech, and Language Processing*, 18(6):1464–1475, 2010.
- [22] M. Parvaix, L. Girin, L. Daudet, J. Pinel, and C. Baras. Hybrid coding/indexing strategy for informed source separation of linear instantaneous under-determined audio mixtures. In *Proceedings of 20th International Congress on Acoustics*, Sydney, Australia, Aug. 2010.
- [23] G.K. Wallace. The JPEG still picture compression standard. *Commun. ACM*, 34:30–44, April 1991.