# ENERGY EFFICIENT CHANGE DETECTION OVER A MAC USING PHYSICAL LAYER FUSION

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## ABSTRACT

We propose a simple and energy efficient distributed Change Detection scheme for sensor networks based on Page's parametric CUSUM algorithm. The sensor observations are IID over time and across the sensors conditioned on the change variable. Each sensor runs CUSUM and transmits only when the CUSUM is above some threshold. The transmissions from the sensors are fused at the physical layer. The channel is modeled as a Multiple Access Channel (MAC) corrupted with IID noise. The fusion center which is the global decision maker, performs another CUSUM to detect the change. We provide the analysis and simulation results for our scheme and compare the performance with an existing scheme which ensures energy efficiency via optimal power selection.

*Key words:* CUSUM, Decentralized Change Detection, Reflected Random Walk, Brownian Approximation, Sensor Networks.

# 1. INTRODUCTION

Sensor networks are often deployed for monitoring and control of systems where human intervention is not desirable or feasible. We are interested in the problem of intrusion detection in a geographical area using sensor networks. The sensor network has the responsibility to detect this intrusion via periodic monitoring of the area and running some algorithm in a distributed fashion. It is assumed that the entry of an intruder will statistically affect the observations taken by the sensors. Thus, the algorithms developed for detection of change ([10, 12]) can be useful.

There are broadly two approaches to change detection ([12], [10]). Shiryaev [12] obtained an optimal algorithm while assuming that the change occurs at a random time with a geometric distribution (this is called the Bayesian setting). Page [10] did not assume any statistics for the unknown time of change, and developed the CUSUM algorithm. This was later shown to be asymptotically optimal in the Min-Max sense in [5]. Moustakides [9] later on showed that it also minimizes the worst case delay.

In our application using sensor networks, two extra issues are involved. One is that the observations are made by many sensors distributed in space. These observations need to be sent to a fusion node to make the final decision. Secondly, each sensor is an inexpensive node with limited computational resources and has very little power. Thus the following variants of the change detection algorithm have been studied in this scenario:

- 1. Each sensor sends a quantized version of its observations to the fusion center. The fusion center, based on the data transmitted, makes a decision on the change ([15, 16]).
- 2. Each sensor runs a test based on algorithms of Shiryaev or Page and performs a local detection. The local decisions are

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then transmitted to the fusion center for it to fuse and make the final decision ([6, 8]).

A specific case of the first version is solved in ([16]) under the Bayesian setting with geometric change variable. If Page's CUSUM is used at each sensor to run the local test and no assumption is made about the change, then [6] has proved that it is asymptotically optimal (in the min-max sense) for the fusion center to declare a change at the first instant at which all the sensors declare a change. Recently [8] has shown that the CUSUM is Min-Max optimal when used in either of the above two scenarios.

In all the above strategies the change detection problem is solved at the link layer, by assuming a perfect physical layer (reliable communication) and energy is conserved by sending fewer bits. The problems with this type of formulation are:

- In all of these approaches the sensor nodes transmit their observations to the fusion node at each time instant. By sending fewer bits the energy is conserved. However in change detection scenarios often the change occurs rarely. One can potentially save considerably by sending observations only when a change is detected by a sensor.
- 2. Even if the communication between the sensor and the fusion center is reliable (this can be ensured for example by using large enough transmit power), the sensors still have to contend at the MAC. With a large number of sensors, this delay can be significant.

In [11], the second effect is mitigated by making decision in each slot at the fusion center by using only the first few bits arriving in the slot. Information from other sensors are ignored. In [7], the information from all the sensors is sent simultaneously using orthogonal codes. In [17], Gaussian MAC is used to fuse the information from different sensors without using orthogonal codes. They also try to minimize directly the energy used in transmission. This provides them with significant gain in performance over the previous studies.

However, because in [17] also, every sensor transmits all its observations, the energy can be saved as mentioned above by sending data only when change occurs.

We propose an energy efficient scheme called DualCUSUM, which uses parametric CUSUM at the sensors (a sensor sends observations only when it senses change by CUSUM), physical layer fusion at the channel (to reduce MAC delay) and one more parametric CUSUM at the fusion center (to exploit all the observations obtained by the fusion center till that time). As compared to [17], we have two improvements: Not sending information from the sensors all the time and using CUSUM at the fusion node, exploiting all past information. No one seems to have used CUSUM at the sensors as well as at the fusion center. We provide a detailed analysis, show that our algorithm is more efficient than that of [17] and obtain an

optimization algorithm to fine tune our algorithm. Furthermore, our algorithm is far more computationally simpler than that in [17] and unlike in [17], we do not require feedback from the fusion node to the sensor nodes.

Section 2 explains the model and introduces the notation. Section 3 analyzes the performance. Section 4 provides the optimization algorithm and Section 5 concludes the paper.

## 2. OUR MODEL AND ALGORITHM

In a geographical area L sensors are deployed providing completely overlapping coverage. Let  $X_{k,l}$  be the observation made at sensor lat time k and it transmits  $Y_{k,l}$ . The fusion center receives at time k,

$$Y_k = \sum_{l=1}^{L} Y_{k,l} + Z_{MAC,k},$$
 (1)

where,  $Z_{MAC,k}$  is iid MAC noise. Observe that this already models the physical layer fusion at the MAC. In practice, for (1) one needs phase, time and carrier synchronization of transmissions from different sensors. Distributed algorithms are available for this.

The distribution of the observations at each sensor changes at a random time T with a known distribution. Before the change  $\{X_{k,l}, k \ge 1\}$  are iid with density  $f_0$  and after the change with density is  $f_1$ . The objective of the fusion center is to detect this change as soon as possible at time  $\tau$  (say) using the messages transmitted from all the L sensors, subject to an upper bound on the False Alarm (FA) probability  $P(\tau < T)$  and the average energy used. Then, the general problem is:

$$\min E_{DD} \stackrel{\triangle}{=} E[(\tau - T)^+],\tag{2}$$

Subj to  $P_{FA} \stackrel{\triangle}{=} P(\tau < T) \le \alpha \& E\left[\sum_{k=1}^{\tau} Y_{k,l}^2\right] \le \mathcal{E}_0, 1 \le l \le L.$ 

Since, sensor observation noise and  $\bar{k}_{1}$  MAC noise are often Gaussian, we will pay particular attention to this case (although all our analysis is valid for general distributions). Then, we will assume that  $X_{k,l} \sim N(\theta_k, \sigma^2)$ , where  $\theta_k = m_0$  before the change and  $\theta_k = m_1$  after the change. Also, then  $\{Z_{MAC,k}\}$ , the MAC noise will be assumed iid Gaussian with mean 0 and variance  $\sigma_M^2$ .

The following algorithm does not provide an optimal solution to (2) but uses several desirable features to provide better performance than the ones we are aware of.

# DualCUSUM

1. Sensor l uses parametric CUSUM (as defined in [10]),

$$W_{k,l} = \max\left(0, W_{k-1,l} + \xi_{k,l}\right), W_{0,l} = 0, \tag{3}$$

where,  $\xi_{k,l} = \log [f_1(X_{k,l}) / f_0(X_{k,l})].$ 

- 2. Sensor *l* transmits in slot *k* only if  $W_{k,l} > \gamma$ . This is the energy saving step.
- 3. Physical layer fusion (as in [17]) reducing transmission delay:

$$Y_k = \sum_{l=1}^{L} Y_{k,l} + Z_{MAC,k},$$
(4)

where,  $Y_{k,l} = b1_{\{W_{k,l} > \gamma\}}, b > 0$  is a design parameter and  $1_A$  denotes the indicator function of set A.

4. Change detection at fusion center via CUSUM:

$$F_{k} = \max\left\{0, F_{k-1} + \log\frac{g_{I}(Y_{k})}{g_{0}(Y_{k})}\right\}$$
(5)

where  $g_0$  is the density of  $Z_{MAC,k}$  and  $g_I$  is the density of  $Z_{MAC,k} + bI$ , I being a design parameter. Thus, for  $Z_{MAC,k} \sim N(0, \sigma_M^2), g_0 \sim N(0, \sigma_M^2)$  and  $g_I \sim N(Ib, \sigma_M^2)$ .

5. The fusion center declares a change at time  $\tau(\beta, \gamma, b, I)$  when  $F_k$  crosses a threshold  $\beta$ :

$$\tau(\beta, \gamma, b, I) = \inf\{k : F_k > \beta\}.$$

Figure (1) compares the optimal DualCUSUM (obtained via the algorithm in Section 4) with the scheme in [17] and the optimal centralized Shiryaev scheme via simulation. We use the parameters:  $L = 2, I = 1, f_0 \sim N(0, 1), f_1 \sim N(0.75, 1), Z_{MAC,k} \sim N(0, 1), T \sim \text{Geom}(\rho = 0.05)$  and  $\mathcal{E}_0 = 7.61$ . Clearly DualCUSUM performs much better than [17] and the performance tends to improve as  $P_{FA}$  decreases. We have also made a limited comparison for 4 sensors. For  $P_{FA} = 5e - 4$  and  $\mathcal{E} = 2.4$  and 3.1, algorithm in [17] gives  $E_{DD} = 24.8$  and 20 while DualCUSUM provided  $E_{DD} = 17.5$  and 16.6 respectively. This motivates us to study DualCUSUM further.



**Fig. 1**.  $\ln(P_{FA})$  (x axis) vs  $E_{DD}$  comparison with [17].

In Section 3, we theoretically analyse DualCUSUM. In Section 4 we provide an algorithm to compute,

$$(\beta^*, \gamma^*, b^*, I^*) = \arg \min_{(\beta, \gamma, b, I)} E_{DD}(\beta, \gamma, b, I)$$
(6)

subj to  $P(\tau(\beta, \gamma, b, I) < T) \le \alpha$  and energy  $\mathcal{E}_{avg}(\beta, \gamma, b, I) \le \mathcal{E}_0$ .

## 3. ANALYSIS

We first provide the false alarm analysis.

## 3.1. Analysis at the Local Sensor

At sensor l,  $Y_{k,l} = b$  only when  $W_{k,l} > \gamma$ . Since  $\{W_{k,l}, k \ge 1\}$  is a reflected Random Walk, with negative drift before the change, the up-crossing of  $\gamma$  by  $W_{k,l}$  can be given by a Poisson process with rate  $\lambda_{\gamma}$  where ([14])

$$\lambda_{\gamma} = \frac{\exp\left[-\sum_{n=1}^{\infty} 2n^{-1} \mathbf{Q}(S_{n,l})\right]}{\int_{-\infty}^{\infty} \left(\log \frac{f_1(u)}{f_0(u)}\right) f_1(u) du} e^{-\gamma},$$
(7)

 $\mathbf{Q}(S_{n,l}) = (\mathbf{P}_{\infty}(S_{n,l} > 0) + \mathbf{P}_1(S_{n,l} \le 0)), \mathbf{P}_{\infty}, \mathbf{P}_1$  respectively representing the probability measures under no change and change at time index 1 and  $S_{n,l} = \sum_{k=1}^{n} \xi_{k,l}$ . For Gaussian  $f_0$  and  $f_1, S_{n,l}$ is Gaussian and hence  $\lambda_{\gamma}$  can be easily computed.

## Distribution of the batch :

Next, we compute the sojourn time of  $W_{k,l}$  above  $\gamma$  after each upcrossing of  $\gamma$  (called a batch size in the following).

Define,  $\nu_{\gamma,l} := \inf\{k \ge 1 : W_{k,l} \ge \gamma\}$ . Note that  $\nu_{\gamma,l} \sim exp(\lambda_{\gamma})$  (equation (7)). The reflected random walk  $\{W_{k,l}\}_{k\ge\nu_{\gamma,l}}^{\tau_{0,l}}$  with  $\tau_{0,l} := \inf\{k : k > \nu_{\gamma,l}; W_{k,l} \le 0\} - \nu_{\gamma,l}$ , is given by an ordinary random walk. Further, with large values of  $\gamma$  (needed for



large  $P_{FA}$ ),  $\tau_{0,l}$  is sufficiently large. Thus, using Donsker's theorem [2] we approximate (with large N):

$$\begin{aligned} \left\{ W_{k+\nu_{\gamma,l},l} \right\}_{k\geq 0}^{\tau_{0,l}} &\sim \left\{ W_{\nu_{\gamma,l},l} + S_{k,l} \right\}_{k\geq 0}^{\tau_{0,l}} \\ &\sim \left\{ W_{\nu_{\gamma,l},l} + \sigma_S \sqrt{N} \zeta \left(\frac{k}{N}\right) + k\mu \right\}_{k\geq 0}^{\tau_{0,l}} \end{aligned}$$

where  $\zeta(t), t \ge 0$  is a standard Brownian motion (BM),  $\mu = E\xi_{1,1}$ and  $\sigma_S = var(\xi_{1,1})$ . Also, we approximate  $W_{\nu_{\gamma,l},l}$  by its mean (which we obtain by using results from [3] and [1]). Then,  $\tau_{0,l}$  is approximated by the time taken by the above BM to reach 0 starting with  $\gamma_{ov} = E(W_{\nu_{\gamma,l},l})$ . This is given by ([4]):

$$P\{\tau_{0,l} > i\} = \Phi\left(\frac{\gamma_{ov} - \mu i}{\sigma_S \sqrt{i}}\right) - e^{\frac{2\mu\gamma_{ov}}{\sigma_S^2}} \Phi\left(\frac{-\gamma_{ov} - \mu i}{\sigma_S \sqrt{i}}\right), \quad (8)$$

where  $\Phi$  denotes the CDF of the standard Gaussian distribution.

We obtain the batch distribution using occupation measure, above  $\gamma$ , of the BM till time  $\tau_{0,l}$  ([13]). Choose time  $t_B$  such that for some small enough  $\epsilon > 0$ ,  $P(\tau_{0,l} \le t_B) > 1 - \epsilon$  and  $P(\nu_{\gamma,l} \ge t_B) > 1 - \epsilon$  $1 - \epsilon$ . This is possible if,  $P[\tau_{0,l} \ll \nu_{\gamma,l}]$  is close to 1, which is true for small  $P_{FA}$  (and hence large  $\gamma$ ).

Define 
$$\delta = E\left(W_{\nu_{\gamma,l},l}\right) / (\sigma_S \sqrt{t_B}), m = \mu \sqrt{t_B} / \sigma_S$$
 and

$$\eta = \#\{k : W_{k,l} \ge \gamma; \nu_{\gamma,l} \le k \le \nu_{\gamma,l} + \tau_{0,l}\}.$$
(9)

The batch size distribution is approximated using [13]

$$P(\{\eta > j\}) = 2 \int_{0}^{j} \left[ \frac{\varphi(m\sqrt{1-u})}{\sqrt{1-u}} + m\Phi(m\sqrt{1-u}) \right] \\ \left[ \varphi\left(\frac{\delta - mu}{\sqrt{u}}\right) \frac{1}{\sqrt{u}} - me^{2m\delta}\Phi\left(\frac{-\delta - m}{\sqrt{u}}\right) \right] du, \quad (10)$$

where,  $\varphi$  represents the standard Gaussian pdf.

We plot these approximations in Figs 2 and 3 which show a good match. This approximation is used in the next section to obtain  $P_{FA}$ . 3.2. False Alarm Analysis

In the DualCUSUM algorithm, transmissions happen only within the batches. Hence, the probability of a FA within a batch is a crucial element in the computation of  $P_{FA}$ . However, FA (at the fusion center) can also occur because of the Gaussian  $\{Z_{MAC,k}\}$  alone. Our approach is to compute the two FAs separately and then combine them in an appropriate way to obtain the  $P_{FA}$ .

3.2.1. Global False Alarm We assume that  $P(\eta << T) \approx 1$  (valid for small  $P_{FA}$ ). By independence of  $\{W_{k,l}\}$  and  $\{W_{k,l'}\}, l \neq l'$ , a batch occurs (at the fusion center) with exponential rate  $L\lambda_{\gamma}$ . Let  $\psi$  represent the number of batches before change. Then, by independence of  $\eta$  and T $P(\psi = j | T = i) = \frac{(L\lambda_{\gamma}i)^{j} e^{L\lambda_{\gamma}i}}{j!}$ . Hence,

$$P_{FA} = \sum_{i=1,j=0}^{\infty} P(FA|T=i; \psi=j) P(\psi=j|T=i) P(T=i).$$
(11)

Let  $\tilde{p}$  denote the FA probability inside a batch. In Section 3.2.3 given below, we will show that the time to FA outside a batch is exponentially distributed with parameter  $\lambda_0$ . Hence, by the assumptions made in this section and by independence of observations,

$$P(FA|T = i; \psi = j) \approx 1 - P(\{\text{No FA in } j \text{ batches } \} (12))$$
  

$$\cap \{\text{No FA in } i \text{ observations}\}|T = i; \psi = j)$$
  

$$\approx 1 - (1 - \tilde{p})^{j} e^{-\lambda_{0} i}.$$

In the above approximation, *i* (minus negligible amount due to batches) observations, with no transmission from any sensor, occur in j + 1batches. But by exponentiality of the distribution,  $P_{FA}$  outside the batches is approximately  $e^{-\lambda_0 i}$ .

If  $T \sim \text{Geom}(\rho)$ , from (11) and (12) we get:

$$P_{FA} = 1 - \frac{e^{-(\lambda_0 + \lambda_\gamma L \tilde{p})} \rho}{1 - e^{-(\lambda_0 + \lambda_\gamma L \tilde{p})} (1 - \rho)}.$$
 (13)

## 3.2.2. False Alarm within a Batch

The false alarm probability within a batch,  $\tilde{p}$  can be computed as,

$$\tilde{p}\approx \sum_{i=1}^{\infty}P(\eta=i)P(\mathrm{FA}\ |\eta=i),$$

where  $\eta$  is the batch size defined in (9) and  $P(\text{FA} | \eta = i)$  represents the probability of FA (CUSUM at the fusion center crossing  $\beta$ ) in *i* transmissions when,  $Y_k = b + \sum_{l=1}^{L-1} Y_{k,l} + Z_{MAC,k}$ . As the batch sizes are small, one can directly calculate it by,

$$P(\text{FA} | \eta = i) = 1 - E \left[ \prod_{k=1}^{i} I_{\{F_k \le \beta\}} \right].$$
(14)

This integral can be computed using Monte Carlo (MC) methods. 3.2.3. False Alarm outside a Batch

In the absence of any transmission from the sensors,  $Y_k \sim N(0, \sigma_M^2)$ . Hence,  $F_k$  is in negative drift. Thus the time to reach  $\beta$ , i.e., time till FA is approximately exponentially distributed with parameter  $\lambda_0$ which can be obtained from [14] as we have done in (7).

# 3.2.4. Comparison of Analysis and Simulation for $P_{FA}$

In this section we tabulate the results obtained for the  $P_{FA}$  by analysis and by simulation. We take  $f_0$ ,  $f_1$ ,  $Z_{MAC,k}$  Gaussian and T Geometric with  $b = 1, m_0 = 0, m_1 = 1, \sigma = \sigma_M = 1$  and provide  $P_{FA}$  values for different values of  $\rho$ ,  $\gamma$ .  $\beta$ , L and I in Table 1.

L	Ι	$\gamma$	β	ρ	$P_{FA}$ Simulation	$P_{FA}$ Analysis
3	1	9	17	0.005	3.66e-5	3.07e-5
3	3	8	15	0.005	3.64e-5	3.95e-5
4	1	10	18	0.0005	1.58e-4	1.29e-4
4	2	9	14	0.005	1.12e-4	1.23e-4
4	4	9	14	0.005	2.21e-5	2.38e-5
4	4	10	17	0.005	1.40e-6	1.29e-6

**Table 1**. Comparison of  $P_{FA}$  obtained via analysis and Simulation: number of sample paths used 10,000,000.

## 3.3. Delay Analysis

The mean detection delay can be written as

$$E_{DD} = E_T \left[ \sum_{k=T}^{\infty} (k-T) P(\{F_k > \beta\} \cap_{n=1}^{k-1} \{F_n < \beta\}) \right], \quad (15)$$

where,  $E_T$  is the expectation w.r.t. the change time T. Since  $E_{DD}$ should be small, after the occurrence of change the drift should be positive. Then, the above integral can be computed using Monte Carlo methods by setting  $F_{T-1}$  and  $W_{T-1,l}$  to the corresponding stationary means. If we take  $F_{T-1} = 0 = W_{T-1,l}$ , then also the approximation obtained is acceptable for reasonably low values of false alarm.

This way of computing  $E_{DD}$  takes negligible computing time as compared to system simulations which run for a long time. We can then use our FA analysis and this computation to obtain the optimal parameters for the DualCUSUM in Section 4.

We are presently working towards getting good approximations or tighter upper bounds for the mean detection delay.

# 4. OPTIMIZATION

Although our optimization algorithm works for general distributions, in the following we limit ourselves to Gaussian distributions and Geometric T. For our choice of parameters we have observed that I = 2 gives the best result. Hence forth, we fix I = 2 and perform optimization only w.r.t.  $(\beta, \gamma, b)$ . Having obtained the analytical expressions (13), (15) for  $P_{FA}$  and  $E_{DD}$  respectively and with average energy given by,

$$\mathcal{E}_{avg} = b^2 \left[ E\left(\tau - \inf_{n \ge T} \left\{ W_{n,1} > \gamma \right\} \right) + \frac{\lambda_{\gamma} L E(\eta)}{\rho} \right], \quad (16)$$

one can use an appropriate optimization technique to solve (6). The term  $E(\tau - \inf_{n \ge T} \{W_{n,1} > \gamma\})$  is computed via Monte Carlo methods as we did for  $E_{DD}$ .

To begin with, for each value of  $\beta$ , we obtain  $(\gamma, b)$  as a fixed point of the two dimensional function (constant *C* is calculated from (7)),

$$h^{\beta}(\gamma, b) := \left[ log\left(\frac{CL\tilde{p}}{log\left(1+\rho\alpha(1-\alpha)^{-1}\right)-\lambda_0}\right), \sqrt{\mathcal{E}_0 b^2 \mathcal{E}_{avg}^{-1}} \right]^T,$$

constructed using the  $P_{FA}$ ,  $\mathcal{E}_{avg}$  constraints (which will be satisfied with equality). We now have a single parameter  $\beta$  and almost unconstrained (of course we will still have positivity constraints) optimization problem. We initially use the grid method (getting the optimal point by exhaustive search over a discretized space) to obtain a coarse optimal point, which is improved upon using a steepest decent algorithm.

We used the above algorithm to obtain the optimal parameters in Table 2 for two different values of L. We set  $L\mathcal{E}_0 = 20$ . The FA constraint used to obtain the optimal parameters  $(\beta^*, \gamma^*, b^*)$  is given in the first column. Table 2 also provides  $P_{FA}$ ,  $\mathcal{E}_{avg}$  of Dual-CUSUM with parameters  $(\beta^*, \gamma^*, b^*)$ . Here we have taken  $F_{T-1} =$  $0 = W_{T-1,l}$ . We see that the theory is matching well with the simulations for low values of  $P_{FA}$  which are of practical concern. This shows the accuracy of approximations in (11) and (15) and of the optimization algorithm. Also we see that even when the total system energy is same (= 20), for four sensors the  $E_{DD}^*$  is much better than for two sensors for the same  $P_{FA}$ .

			Analysis	Simulation
$\alpha$	L	$(eta^*,\gamma^*,b^*)$	$E_{DD}^*$	$(P_{FA}, E_{DD}^*, \mathcal{E}_{avg})$
5e-5	2	(15.17, 7.88, .69)	47.59	(4.7e-5, 47.06, 10.05)
1e-5	2	(16.54, 8.13, .60)	55.60	(1.1e-5, 55.04, 10.01)
5e-5	4	(21.00, 6.76, .71)	30.0	(4.0e-5, 29.80, 05.02)
1e-5	4	(22.00, 7.32, .65)	34.3	(0.9e-5, 34.02, 05.01)

**Table 2**. Performance of Optimal DualCUSUM : Comparison of simulation with analysis for  $m_0 = 0$ ,  $m_1 = 0.75$ ,  $\sigma_S = 1$ ,  $\sigma_M = 1$ ,  $\rho = 0.005$ , I = 2 and  $L\mathcal{E}_0 = 20$ , .

# 5. CONCLUSIONS AND FUTURE WORK

We have proposed a Page's CUSUM based energy efficient scheme which uses the physical layer fusion technique and CUSUM at the sensors as well as at the fusion center. We have analyzed the FA performance of the scheme and computed the approximate mean delay using Monte Carlo techniques. The analytical results obtained give us a good approximation which can be used to choose the optimal parameters. We have also compared our scheme with the scheme proposed in [17] for a fixed energy constraint. The comparisons show that our scheme saves a lot more energy for small values of FA and uses it to improve on the detection delay.

At present we are working towards good approximations for  $E_{DD}$ , and some variants of DualCUSUM, and some analytical way of solving for the optimal choice of parameters.

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