CODING OF PREDICTION RESIDUAL IN MPEG-4 STANDARD FOR LOSSLESS AUDIO CODING (MPEG-4 ALS)

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ABSTRACT

We describe two alternative schemes for encoding of prediction residual adopted in the MPEG-4 ALS standard for lossless audio coding. We explain choices of algorithms used in their design and provide both analytical and experimental analysis of their performance.

1. INTRODUCTION

Working draft of the specification ISO/IEC 14496-3:2001/AMD 4 (MPEG-4 ALS) [8] represent the latest planned addition to a suite of MPEG Audio standards [5], defining technology for lossless coding of PCM audio signals.

In a nutshell, MPEG-4 ALS is a forward-adaptive Linear Predictive Coder (LPC) in which predicted signal is quantized to the resolution of the input PCM signal. Combined with lossless compression and transmission of quantized filter coefficients and the residual this insures lossless reconstruction of the original signal.

The structure of this algorithm is shown in Fig.1. It contains all standard building blocks of an LPC coder: buffer for storing blocks of input PCM signal, prediction filter, module for estimation and quantization of filter coefficients, entropy coding and multiplexing units. Specific features of MPEG-4 ALS encoder include its ability to change order of the predictor, use different block sizes, inject headers insuring random access to compressed data, etc.

In this paper we will describe two alternative techniques used in this algorithm for encoding of prediction residual. The first scheme, provided in the first reference model of MPEG-4 ALS [8] is based on the use of simple parametric Golomb-Rice codes [4, 16]. The other scheme, accepted as a first core experiment [14] is more complicated, and it uses several coding techniques, such as block Gilbert-Moore, fixed-length, and Golomb-Rice codes.

In describing these schemes our main goal will be to explain the choices of coding algorithms and parameters used in their design. We will complement our exposition by presenting experimental results.

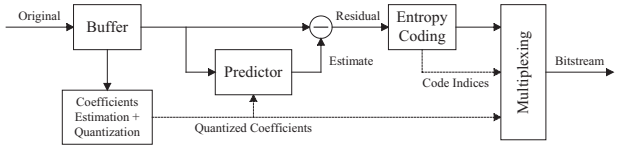

Fig. 1. MPEG-4 ALS encoder.

2. RICE CODING OF PREDICTION RESIDUAL

Golomb codes [4] represent a special case of Huffman codes constructed for sources with geometric distribution of symbols: $\Pr\{r_\theta = i\} = (1-\theta)\,\theta^i$ where $\theta \in (0,1)$. The code $G_m(i)$ consists of a series of k ones, where k is the result of a division $k = \lfloor i/m \rfloor$, followed by a 0-bit, and a $\lceil \log_2 m \rceil$-bit representation of the remainder $i \mod m$. It has been shown (see [4, 2]) that an optimal for a source r_θ parameter m can be calculated as follows:

$$m = \lfloor -\log(1+\theta) \,/\, \log\theta \rfloor \,. \tag{1}$$

If this quantity is further rounded to the nearest power of 2, then the divisions can be replaced by shifts, resulting in an extremely simple and fast encoding. The codes $GR_s(i) := G_{2^s}(i)$ are often called Golomb-Rice or Rice codes [16] with parameter s.

Robinson [19] has already observed that the distribution of the residual signal in LPC-based audio encoders can be closely modelled by a Laplacian (or two-sided geometric) distribution. This means, that in order to apply Golomb-Rice codes one simply needs to flip the negative side of the distribution and merge it with the positive one. In MPEG-4 ALS this is accomplished by a mapping:

$$r_i^+ = \begin{cases} 2\,r_i & \text{if } r_i \geqslant 0\,, \\ -2\,r_i - 1 & \text{if } r_i < 0\,. \end{cases} \tag{2}$$

In order to estimate the optimal Golomb-Rice parameter s for a block of residuals $r_1, \ldots, r_n$, the reference implementation of MPEG-4 ALS calculates their absolute mean:

$$\mu_n = \frac{1}{n}\sum_{i=1}^{n} |r_i| \,, \tag{3}$$

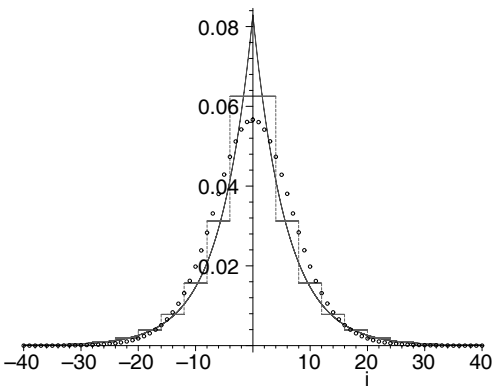

Fig. 2. Observed residual distribution (circles), Laplacian distribution (solid line), and the distribution corresponding to the lengths of Golomb-Rice codes (dashed line).

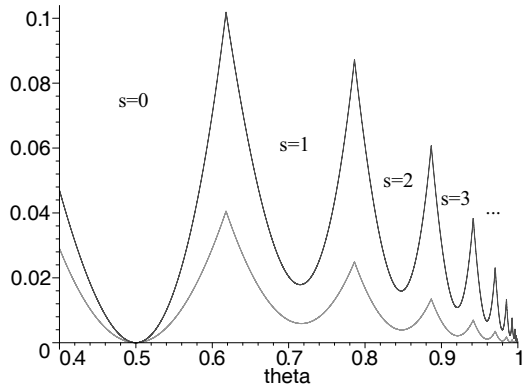

Fig. 3. Redundancy $R^{GR}(x_\theta) = E\{|GR_s(x_\theta)|\} - H(x_\theta)$ and normalized redundancy $R^{GR}(x_\theta)/H(x_\theta)$ of Golomb-Rice codes for a source x_θ: $\Pr\{x_\theta = i\} = (1-\theta)\,\theta^i$.

and then uses:

$$s = \lfloor \log_2 \mu_n + C_1 \rfloor \ , \tag{4}$$

where $C_1 \approx 0.97$ is a constant.

This estimator has already been used in compression algorithms such as SHORTEN [19] or LOCO-1 [24], and it is based on the fact that sample absolute mean μ_n converges (with large n) to the first absolute moment $E\{|r|\}$ of the distribution. Thus, in a Laplacian model: $E\{|r|\} = \int_{-\infty}^{\infty} \Pr\{r=\rho\}\,|\rho|\,d\rho = \int_{-\infty}^{\infty} \frac{1}{\sqrt{2}\lambda}\, e^{-\frac{\sqrt{2}}{\lambda}|\rho|}\,|\rho|\,d\rho = \frac{1}{\sqrt{2}}\lambda$, where λ is the variance. In turn, λ can be converted in a parameter θ of the quantized geometric distribution, and then by (1), setting $s = \log_2 m$, and ignoring smaller than $O(1)$ terms we arrive at (4).

Obtained in such a way code parameter s is transmitted along with the encoded residuals $GR_s\left(r_1^+\right), \ldots, GR_s\left(r_n^+\right)$. To facilitate a higher degree of adaptation during transients in audio signals MPEG-4 ALS includes a mode in which each block is divided in several smaller sub-blocks encoded using different (individually estimated for each sub-block) code parameters.

In Fig.2 we show a typical observed distribution of the residual, its approximation by a Laplacian distribution, and the distribution corresponding to the lengths of the resulting Golomb-Rice codes. It is clear there is a divergence between the observed distribution and one that is being encoded. However, after an extensive experimental study [13] using MPEG audio sequences [6] we have found that the estimated average redundancy of Golomb-Rice encoding represents only $1.6452..\%$ of the bitrate occupied by the residuals. In other words, given the simplicity of this coding scheme, it works remarkably well in this application.

3. IMPROVED RESIDUAL CODING

The main motivations for including another residual coding scheme in MPEG-4 ALS were: a) the requirement to achieve a better compression than what is claimed by today's state of the art algorithms [6], b) realization of the fact that the efficiency of encoding of residuals is critical for the performance of the entire algorithm, and c) the fact that Golomb-Rice codes have fundamental performance limits (see [2, 23], also Fig.3), hence further progress cannot be achieved without using a more efficient technique.

On the other hand, looking for alternative schemes we also had to consider their complexity, so our final goal was to design an algorithm that substantially reduces the redundancy of encoding of prediction residuals while making the whole encoding/decoding process only slightly more complex [14].

In order to achieve this goal, the following techniques have been incorporated.

3.1. Higher-resolution representation of parameter s.

Similar to the previous scheme, at the beginning of each block we transmit parameter s describing the probability distribution of the residuals. We use the same technique for estimation of this parameter, but we quantize and transmit it using higher precision.

3.2. Partition of the residual distribution.

To restrict memory usage we only construct high-efficiency block codes for a central region $[-r_{\max}, r_{\max}]$ of the residual distribution (see Fig.4). The tails are still encoded using Golomb-Rice codes as described in the previous section.

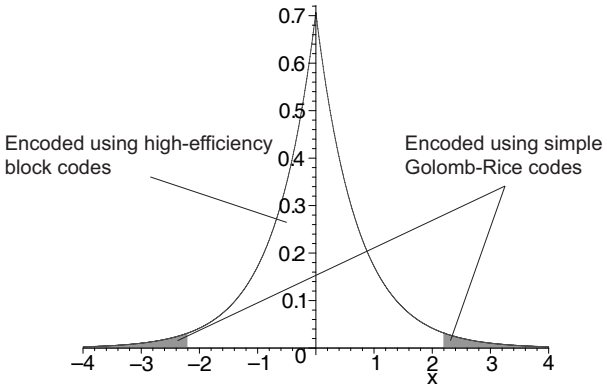

Fig. 4. Partition of the residual distribution.

3.3. The use of block Gilbert-Moore codes for nested ordered distributions.

To encode residual values in the central region we have chosen to use block Gilbert-Moore codes [3]. The key advantages of these codes[1] come from the facts that:

- their average redundancy rate is *decreasing with the length of an encoded block* (cf. [3, 9, 23]):

$$R^{GM}(n) = \frac{3/2+\delta(n)}{n} < \frac{2}{n}, \tag{5}$$

  where n is the block length, and $\delta(n)$ is an oscillating function of bounded magnitude $|\delta(n)| < 1/2$.

- they can be approximately constructed using memory-efficient arithmetic encoders [17, 12, 18, 25]. The added redundancy of such an implementation with m-symbols alphabet, t-bit code registers, and τ-bit probability representations is bounded by [22]:

$$R^{AC}(t,\tau) < m\,(\tau + \log e)\; 2^{-(t-2)} \tag{6}$$

  and can be easily controlled by properly selecting t and τ.

- the construction of these codes is based on cumulative probabilities of symbols, making it possible not only to encode a source with a given distribution, but also *all reduced-resolution versions of this source*.

For example, given symbols $a_1, \ldots, a_m$ with non-increasing probabilities $p_1 \geqslant \ldots \geqslant p_m$, the code construction requires a table with m quantities $s_i = \sum_{j=i}^{m} p_j$. If we now quantize this source, for example, by skipping the last bit, then the new symbols $\hat{a}_1, \ldots, \hat{a}_{\lfloor m/2 \rfloor}$ will have (also non-increasing) probabilities $\hat{p}_i = p_{2i} + p_{2i+1}$. It is clear, that the new cumulative probabilities $\hat{s}_i = s_{2i}$ simply represent a *sub-set of the same table* $s_1, \ldots, s_m$. As a general rule, if Δ represents the number of skipped bits, then the encoding of such symbols can be accomplished by using probabilities $\hat{s}_i = s_{i\,2^\Delta}$.

[1] Sometimes these codes are also called Elias-Shannon-Fano codes [1].

3.4. Block-size adaptive reduction of the alphabet size.

In order to speed up both encoding and decoding and to further reduce memory usage we split and transmit k least significant bits (LSBs) of the residuals in central region directly[2]. The number of directly transmitted bits k is selected using:

$$k = \begin{cases} 0, & \text{if } s \leqslant B\,, \\ s - B, & \text{if } s > B\,, \end{cases} \tag{7}$$

where s is the code parameter (4), and B is a quantity depending on the block size n:

$$B = \lfloor (\log n - 3)\,/2 \rfloor\ . \tag{8}$$

The associated parameter Δ (the number of missing bits) used in our Gilbert-Moore encoder is obtained using:

$$\Delta = 5 - s + k\,, \tag{9}$$

where 5 is the maximum value of B, given that MPEG4 ALS's block size $n \leqslant 2^{13}$.

By using Laplacian model of residual distribution it can be shown that the described choice of the parameter k limits the redundancy due to direct transmission of LSBs to approximately $\frac{2}{3\,n}$, which has the same speed of convergence (with the block size n) as our Gilbert-Moore codes (5), and represents only 25% of the combined redundancy of codes in the central region. Choices of other parameters in our algorithm, such as $r_{\max}$, t, and τ, are also based on similar constrains, leading to only minor increase in the total redundancy of this scheme.

Overall, our implementation of the improved residual coding scheme uses only 2K words of memory to store probability tables, and involves 2 multiplications per encoded or decoded sample. Given the fact that the order of the prediction filter in MPEG-4 ALS typically fluctuates in the range of $8 - 16$, these two extra multiplications have only minor (limited to $12.5 - 25\%$) effect on the overall performance.

4. EXPERIMENTAL RESULTS

The results of our experimental study are summarized in Table 1. The test material was taken from the standard audio sequences for MPEG-4 Lossless Coding [6]. It comprises nearly 1 GB of stereo waveform data with sampling rates of 48, 96, and 192 kHz, and resolutions of 16, 20, and 24 bits.

The column "compression" in Table 1. contains ratios of compressed file sizes to the sizes of original waveform files, expressed in %s. Both compression and decompression speeds are measured in seconds. To run these tests we used a PIII-M computer with 500M bytes of RAM.

In these tests we used reference-model implementation of the MPEG-4 ALS encoder [11].

[2] This idea is similar to the "alphabet grouping" technique [21], but our approach is much simpler because we use groups of equal size.

Format	Compression		Enc. Time		Dec. Time	
	RM0	*CE1*	*RM0*	*CE1*	*RM0*	*CE1*
48kHz-16	46.8	46.3	44.7	55.8	17.3	24.5
48kHz-20	64.2	63.9	60.9	58.5	25.6	26.3
48kHz-24	64.2	63.9	62.4	58.5	24.8	26.3
96kHz-16	31.3	30.7	77.4	104.4	31.9	44.8
96kHz-20	50.2	49.9	114.9	117.0	46.9	52.2
96kHz-24	48.8	48.4	109.7	116.5	47.5	52.0
192kHz-16	22.3	21.6	59.3	76.1	24.9	33.3
192kHz-20	42.3	41.9	88.7	100.2	50.7	53.2
192kHz-24	39.5	39.0	91.3	99.7	47.9	51.8
Total	**45.2**	**44.7**	**709.3**	**786.8**	**317.4**	**364.2**

Table 1. Performance analysis for different audio formats. Algorithm *RM0* uses Golomb-Rice codes, while algorithm *CE1* uses improved residual coding scheme.

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