# Rapid Design of Discrete Orthonormal Wavelet Transforms using Silicon IP Components

Shahid Masud *Student Member IEEE* and John V. McCanny *Senior Member IEEE* DSiP™ Laboratories, School of Electrical Engineering and Computer Science, The Queen's University of Belfast, Stranmillis Road, Belfast BT9 5AH, Northern Ireland Email: Shahid.Masud@ee.qub.ac.uk

#### Abstract

A rapid design methodology for orthonormal wavelet transform cores has been developed. This methodology is based on a generic, scaleable architecture utilising time-interleaved coefficients for the wavelet transform filters. The architecture has been captured in VHDL and parameterised in terms of wavelet family, wavelet type, data word length and coefficient word length. The control circuit is embedded within the cores and allows them to be cascaded without any interface glue logic for any desired level of decomposition. Case studies for stand alone and cascaded silicon cores for single and multi-stage wavelet analysis respectively are reported. The design time to produce silicon layout of a wavelet based system has been reduced to typically less than a day. The cores are comparable in area and performance to hand-crafted designs. The designs are portable across a range of foundries and are also applicable to FPGA and PLD implementations.

# 1. Introduction

The design for 'reuse' methodology is being considered as the only way forward for designing complex dsp hardware. This methodology reduces the time-to-market through the use of silicon cores or mega-cells in the VLSI design of a digital signal processing chip. The value of a silicon core is based on its reusability which in turn is based on the degree of parameterisation envisaged in the design process. Thus for all new applications, a component does not need to be designed from scratch leading to a reduction in design time and development expenditure and an improvement in design quality [1]. A considerable skill in the development of silicon cores is required so as to provide an efficient architecture along with comprehensive reusability. Due to this aspect, the silicon cores are also widely cited as *Intellectual Property Components*.

The description of complex circuits through VHDL has created a paradigm shift in the ASIC design process. Not only does it allow various architectural templates of dsp functional components to be described at different levels of abstraction, the components can be parameterised in a variety of dimensions and functionally tested within the VHDL environment. Also, the adoption of IEEE standard for VHDL has enhanced its portability across a range of commercial synthesis and simulation tools [2].

This paper presents the application of VHDL based 'reuse' methodology for the implementation of discrete wavelet transforms. A brief overview of wavelet transforms is presented in section 2. This is followed by a discussion on their implementation. A rapid design strategy for wavelet transforms implementation is presented in section 3. Several case studies are reported in section 4 followed by the summary and conclusions.

# 2.0 Discrete Wavelet Transforms

The use of wavelet transforms is becoming increasingly popular in speech and image processing applications. The main advantages in using a wavelet transform is the non-block based signal decomposition along with the fact that the transformed coefficients are localized in both space and frequency thus providing a multi-resolution analysis.

A discrete wavelet transform performs a multi-stage signal decomposition using a filter bank structure shown in figure 1. The filter bank comprises a lowpass and a highpass filter, each followed by decimation by two. The decimated lowpass output from the preceding stage acts as the filter-bank input for the succeeding stage and so on. Accordingly, any number of stages can be cascaded to produce a wavelet based decomposition. From a practical perspective, a three stage decomposition is considered adequate in most applications.



Fig 1: A three level wavelet decomposition system

The hardware implementation of discrete wavelet transforms is quite demanding in terms of circuit area requirements [3]. Also, the varying sample rate at every stage adds to the complexity of the control circuit. However, from a VLSI perspective, the interesting aspect is the similarity in architecture of the filter banks required. An efficient architecture and design of a single level decomposition allows 're-use' of the same in subsequent stages, albeit at different sample rates and different word lengths.

To date, most of the implementation schemes have been based on biorthogonal type of wavelet functions [4] mainly because symmetry in filter coefficients can be exploited to reduce the number of multipliers. Moreover, some biorthogonal wavelet filter afford integer coefficients which makes the system design even simpler [5]. Orthonormal wavelets, which are the subject of this paper, offer important signal processing properties such as regularity and higher vanishing moments which are desirable in many applications. The orthonormal filters have un-symmetric, real number coefficients which can make their implementation more complex. The purpose of this paper is to describe architectural synthesis and methods for the rapid silicon design [6, 7] of a very broad range of orthonormal wavelet transforms. A key aspect has been the development of a canonic architecture which is scaleable and can be applied to any general orthonormal wavelet transform. Previous attempts at simplifying the implementation of orthonormal wavelets have mostly been directed towards specific wavelets such as 'Daubechies' wavelet functions [8, 9]. Such architectures are not universal and can only be used in very specific applications.



# a 8 taps wavelet filter

References [10, 11, 12] contain a comprehensive overview of the architectural approaches for wavelet transforms. The generic architectural block developed for the illustration of our rapid design methodology is shown in figure 2. It is a canonic implementation of decimated filters and offers very high efficiency in terms of computation and area [13]. This scheme is derived from bi-phase decomposition of wavelet analysis filters through which, the even and odd samples are separately processed and the accumulated result is produced after processing two consecutive samples.

We have focused our effort on high throughput applications and consequently a bit-parallel, word-serial filter implementation has been assumed (although the architecture can also be simply extended to other word formats, such as bit-serial or digit serial data).

# 3. Rapid Design of Wavelet Cores

A detailed analysis of orthonormal wavelet families suggests that all of these wavelets can be suitably implemented using a filter bank structure. These wavelets differ in the choice of filter coefficients and the number of taps of the filter. A flexible and area efficient scheme must be able to scale the architecture on the fly based on generic specification of required wavelet family. Moreover, due to the nature of wavelet transforms and the fact that new wavelet transforms are continually being reported in literature, we should be able to add a new wavelet family whenever required.

The architecture presented in figure 2 is broken into three parts as shown in figures 3 to 5. The *input* component in figure 3 is the first part of the filter. It comprises a multiplier and a delay. The delay is incorporated to synchronise the data read-in and hence it facilitates the seamless interfacing of multiple wavelet core blocks.





The second component represents the *repeating taps* of the filter. The presence of two delays signify the difference between an ordinary FIR filter and the decimated approach that we have adopted. The other elements in this block are a multiplier/adder (MAC). This component directly interfaces to the *input, output* or an identical block.



Wavelets Package

The *output* block represents the accumulator and decimator. The output is only available when two samples have been processed.

The control circuit and coefficient scheduling mechanism is a part of the core block. The only external signals required for complete functioning are *Clock* and *Reset*. The *Clock* signal also directly determines the sample frequency.

The methodology allows us to rapidly explore the design space by incorporating appropriate multiplier / accumulator components from a synthesizable library. Means are provided whereby specific hardware instantiations captured

using hierarchical VHDL blocks can be simulated and compared with MATLAB results to assess finite word length effects and allocated appropriate word lengths for cascading blocks.



Fig 5 : The 'output' component in Wavelets Package

Each of these functional parts has been parameterised in terms of word length and overflow bits. These correspond to sign extension in 2's complement arithmetic. The blocks were developed using synthesizable components from VHDL libraries supplied by ISS Ltd [6]. Specifically, a Booth encoded, Wallace tree multiplier, a carry-save adder and asynchronous clear Dflip-flops were used to develop these core processing blocks. The architecture based on these synthesizable blocks can be extended during synthesis to cater for any wavelet family and type.

There is no direct mechanism in VHDL to acquire the wavelet coefficients from a high level description. Also, the coefficients cannot be supplied at the time of instantiation because only 'integers' are permitted as generic parameters. The following method was therefore developed to incorporate a range of wavelet families through a generic description.

A MATLAB code was used to generate a text file containing the coefficients for any desired wavelet. Some of the commonly used wavelet coefficients are now available over the Internet [14]. These can be directly used in our scheme. The use of a numerical package offers un-limited possibilities regarding the choice and future development of wavelets. The text file containing real number coefficients is converted to 2's complement format at 16 bits resolution using VHDL code. The coefficients are then appropriately placed in a VHDL package. The required word length specified in the generic description is chosen at the time of instantiation. Each wavelet is identified by a separate number which is specified in generics to access those coefficients. Addition of a new wavelet is trivial and involves repeating these steps. Table 1 shows a few entries in the coefficients package.

 Table 1: Entries of Wavelet Coefficients in

 VHDL Package

Generic Number	Wavelet Type
1	Daubechies 8 taps
2	Symmlet 12 taps
3	Daubechies 4 taps
4	Morlet
5	Coiflet1
6	Coiflet2

# 4. Design Case Studies

Numerous design examples have been undertaken to illustrate the ease and speed with which wavelet transforms can be implemented. The methods presented allow a non-specialist DSP engineer to develop a silicon implementation of a full wavelet system in parallel with algorithm development. The following generic parameters are all that need to be specified at the time of instantiation of any wavelet block:

- 1. Data word length,
- 2. Coefficient word length,
- 3. Word length extension to prevent overflow (and to cater for cascading stages),
- 4. Wavelet family,
- 5. Values for taps (or type) of the filter required.

The performance measures, especially power and area, reported for each core are purely relative. They are entirely dependent on chosen wordlengths and wavelet type. The cores can be cascaded to produce a multi-level and multi-dimensional wavelet analysis or used in a stand-alone fashion alongside memory and multiplexers as shown in figure 6. The block Qr in this figure represents the word length constraints in the data path.





4.1 Daubechies 4 taps wavelet analysis, three stages

A three level wavelet decomposition based on a Daubechies 4 taps wavelet, a replica of figure 1, was synthesised using Synopsys<sup>TM</sup> environment. The layout was generated using Compass Design Automation<sup>TM</sup> tools. The coefficient resolution in 2's complement format was set at 7 bits and the data resolution was 9 bits. A 6 bit truncation was applied after every stage so that the internal word length was 18 bits, 21 bits and 24 bits for first, second and third stage respectively. The resulting layout is shown in figure 7. This is for a triple level metal, 0.35 $\mu$  CMOS technology. The silicon area required in this case is 1.5 mm<sup>2</sup>. The number of transistors required for this design are 74 K (~20 K gates). The maximum sample rate was found to be around 100 MHz with a typical power dissipation of less than 300 mW.

#### 4.2 Symmlet 12 taps wavelet analysis, two stages

In this case a two level wavelet decomposition based on a Symmlet 12 taps wavelet was synthesised. The coefficient resolution in 2's complement format was set at 10 bits and the data resolution was 9 bits. The internal word length accuracy was 25 bits and 32 bits for the first and second stage

respectively using a 9 bit truncation between the two stages. The silicon area required in this case is  $2.19 \text{ mm}^2$  (1.19 mm x 1.84 mm). The core requires 110 K transistors (~35 K gates). Typical power dissipation for this core at 100 MHz data throughput is around 600 mW.



Fig 7 : The silicon layout for Daubechies 4 taps, 3 level wavelet analysis

#### 4.3 Rapid Prototyping on FPGAs

The layout for a Xilinx 4000 series FPGA was produced using fpga\_analyzer<sup>™</sup> and Design Manager<sup>™</sup> toolsets. The total time to generate the layout was less than a day. The design comprises 353 Configurable Logic Blocks (CLB) and 50 Input/Output Blocks (IOB) for 8 bits data and 7 bits coefficient resolution for Daubechies 8 taps wavelet analysis. The clock rate targeting an XC4025E, speed grade-4 device was found to be of the order of 30 MHz. This is sufficient for carrying out a three level wavelet transform of a 256x256 pixels image at 25 frames/sec using the configuration shown in figure 6.



Fig 8: The XC4025-4 FPGA floorplan for Daubechies 8 taps wavelet transform processor

# 5. Conclusion

A method for the rapid design and implementation of discrete orthonormal wavelet transforms has been developed. The approach allows a non-specialist to implement a wide range of wavelet transform based systems directly in silicon. A new wavelet family can easily be added whenever required to give additional flexibility to the design space. The implementation is independent of silicon technology and can easily be ported to FPGAs and PLDs. An efficient architecture for the decimated filters was chosen as the basis of the generator presented. This has been parameterised in terms of word lengths so that the same block can be 're-used' in a multi stage wavelet analysis system. The results obtained from three synthesis examples given in the paper demonstrate the effectiveness of this approach.

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